

**O‘ZBEKISTON RESPUBLIKASI OLIY VA O‘RTA
MAXSUS TA’LIM VAZIRLIGI**

TOSHKENT DAVLAT TEXNIKA UNIVERSITETI

“TASDIQLAYMAN”

O‘quv ishlari bo‘yicha prorektor

_____ O.O.Zaripov

“ ____ ” _____ 2019 yil

“OLIIY MATEMATIKA” KAFEDRASI

Sirtqi ta’lim yo’nalishlari uchun

OLIIY MATEMATIKA

fanidan

TOPSHIRIQLAR TO’PLAMI-3

Toshkent – 2019

Ushbu sirtqi ta'lim yo'nalishi talabalari uchun tuzilgan topshiriqlar to'plami oliy matematika fanining qatorlar, karrali integrallar va egri chiziqli integrallar bo'limlarini o'z ichiga olgan. Fanning ko'rsatilgan bo'limlaridan talabalar uchun nazariy va amaliy topshiriqlar tuzilgan.

Ushbu topshiriqlar to'plami mashinasozlik fakultetining "Oliy matematika" kafedrası majlisida (**2019yil " " -son bayonnoma**) muhokoma etildi.

"Oliy matematika"
kafedra mudiri

_____ dots. Sh.T. Pirmatov

"Oliy matematika" kafedrası kotibi

_____ kat.o'q. G. Abdikayimova

Ushbu topshiriqlar to'plami universitetning Ilmiy-uslubiy kengashida ko'rib chiqildi va tasdiqlandi. (**2019 yil " " _____ - son bayonnoma**).

O'quv uslubiy boshqarma boshlig'i

_____ N. Mambetov

3-tipik hisob

Nazariy savollar

1. Sonliqatorlar. Musbat hadli qatorlarning yaqinlashish va uzoqlashish beigilari.
2. Funksional qatorlarularning yaqinlash ishsohasi.
3. Darajali qatorlar.
4. Funksiyalarni Teylor va Makloren qatorlariga yoyish.
5. Darajali qatorlarning tadbiqlari.
6. Fur'e qatorlari.
7. Dekart koordinatalarida ikki o'lchovli integrallarni hisoblash.
8. Dekart koordinatalarida uch o'lchovli integrallarni hisoblash.
9. Ikki va uch o'lchovli integrallarda o'zgaruvchilarni almashtirish hamda ularning tadbiqlari.
10. Birinchi va ikkinchi tur egrichiziqli integrallar hamda ularning tadbiqlari.

Bajarish uchun vazifalar.

- 1– vazifa.** Qatorlarning yaqinlashuvchi ekanini isbot qiling va ularning yig'indisini toping.
- 2– vazifa.** Dalamber va Koshi belglaridan foydalanib quyidagi qatorlarning yaqinlashish yoki uzoqlashishini tekshiring.
- 3– vazifa.** Integral belgidan foydalanib quyidagi qatorlarni yaqinlashishga tekshiring.
- 4 – vazifa.** Quyidagi qatorlarni Leybnits belgidan foydalanib yaqinlashuvchilikka tekshiring va yaqinlashish turini aniqlang.
- 5 – vazifa.** Darajali qatorlar. (1-15). Quyidagi qatorlarni yaqinlashish radiusini toping. (16-30). Quyidagi qatorlarni yaqinlashish sohasini toping.
- 6 – vazifa.** Teylor va Makloren qatorlariga yoying.
- 7– vazifa.** Quyidagi keltirilgan sonlarni berilgan ε aniqlikda hisoblang.
- 8 – vazifa.** Funksiyani berilgan oraliqlarda Fur'e qatoriga yoying.
- 9 – vazifa.** Integrallash tartibini o'zgartiring.
- 10 – vazifa.** (1-22) Ikkikarrali integralni hisoblang. (23-30) Berilgan chiziqlar bilan chegaralangan jism hajmini hisoblang.
- 11 – vazifa.** Uch o'lchovli integrallarni hisoblang.
- 12 – vazifa.** Birinchi tur egri chiziqli integralni hisoblang.
- 13 – vazifa.** Ikkinchi tur egri chiziqli integralni hisoblang.

1 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{(2n-1)(2n+1)}$$

$$2. \sum_{n=1}^{\infty} \frac{n^n}{n! \cdot 2^n}$$

$$3. \sum_{n=1}^{\infty} \frac{1}{n(1+\ln n)}$$

$$4. \sum_{n=1}^{\infty} (-1)^n \cdot \frac{1}{n}$$

$$5. \sum_{n=1}^{\infty} \frac{(x)^n}{2^n}$$

6. $f(x) = x^5 - 4x + 2x^3 + 2x + 1$ ko'phadni $(x+1)$ ikki hadning darajalari bo'yicha yoying.

$$7. \cos 18^\circ, \varepsilon = 0,001$$

8. $f(x) =$
 $\begin{cases} -2x, & \text{agar } -\pi \leq x < 0 \text{ bo'lsa,} \\ 3x, & \text{agar } 0 \leq x \leq \pi \text{ bo'lsa.} \end{cases}$ Ushbu funksiyani Fur'e qatoriga yoying.

$$9. \int_{-2}^{-1} dy \int_{-\sqrt{2+y}}^0 f dx + \int_{-1}^0 dy \int_{-\sqrt{-y}}^0 f dx.$$

$$10. \int_0^1 \int_1^2 \frac{1}{(x+y)^2} dx dy$$

$$\iiint_V 15(y^2 + z^2) dx dy dz :$$

$$11. (V) : \begin{cases} z = x + y, & x + y = 1; \\ x = 0, & y = 0, & z = 0. \end{cases}$$

12. $I = \int_{\gamma} xy dl$, buyerda γ -uchlari A(-2; -2), B(6; 1), C(2; 5) nuqtalardabo'lgan uchburchak konturi.

13. $I = \int_{\gamma} \frac{y^2 dx - x^2 dy}{x^2 + y^2}$, buyerda γ -yarimaylana:
 $x = a \cos t, y = a \sin t, 0 \leq t \leq \pi$.

2 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{(3n-2)(3n+1)}$$

$$2. \sum_{n=1}^{\infty} \frac{(3n-2)!}{((n+1)!)^3}$$

$$3. \sum_{n=1}^{\infty} \frac{1}{\sqrt{6n+5}}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n-2}$$

$$5. \sum_{n=1}^{\infty} (n+1)x^n$$

6. $f(x) = x^4 - 5x^3 + x^2 - 3x + 4$ ko'phadni $(x-4)$ ikki hadning darajalari bo'yicha yoying.

$$7. \cos 36^\circ, \varepsilon = 0,001$$

8. $f(x) = x^2$ funksiyani $-\pi \leq x \leq \pi$ oraliqda Fur'e qatoriga yoying.

$$9. \int_0^1 dy \int_{-\sqrt{y}}^0 f dx + \int_1^{\sqrt{2}} dy \int_{-\sqrt{2-y^2}}^0 f dx.$$

$$10. \int_0^{2\pi} \int_1^{2+\sin x} \frac{y}{2} dx dy$$

$$\iiint_V 5x^2 dx dy dz :$$

$$11. (V) : \begin{cases} 4x + 3z = 1, & y = 4; \\ x = 0, & y = 0, & z = 0. \end{cases}$$

$$12. I = \int_{\gamma} x^2 dl, \text{ buyerda } \gamma -$$

birinchichorakdagi $8y^2 = x^3$ egrichiziqning $y^2 = 2x$ parabola bilan ajratilgan qismi.

$$13. I = \int_{\gamma} (2a-y) dx - (a-y) dy, \text{ buyerda } \gamma -$$

γ -sikloidaning birinchiarki:
 $x = a(t - \sin t), y = a(1 - \cos t), 0 \leq t \leq 2\pi$

3 – variant

$$1. \sum_{n=1}^{\infty} \frac{3^n + 2^n}{6^n}$$

$$2. \sum_{n=1}^{\infty} \frac{(n!)^2}{(2n)!};$$

$$3. \sum_{n=1}^{\infty} \frac{3}{n^2 + 4}$$

$$4. \sum_{n=1}^{\infty} (-1)^n \cdot \frac{1}{n^2}$$

$$5. \sum_{n=1}^{\infty} \frac{(x)^n}{n}$$

$$6. f(x) = \frac{1}{x+1} \text{ funksiyani}$$

Makloren qatoriga yoying.

$$7. \cos 72^\circ, \varepsilon = 0,001$$

8. $f(x) = x$ funksiyani $-\pi \leq x \leq \pi$ oraliqda Fur'e qatoriga yoying.

$$9. \int_0^1 dy \int_0^y f dx + \int_1^{\sqrt{2}} dy \int_0^{\sqrt{2-y^2}} f dx.$$

$$10. \int_0^4 \int_y^2 (3x^2 - 2xy + y) dx dy$$

$$11. \iiint_V \frac{dx dy dz}{1 + \frac{x}{3} + \frac{y}{4} + \frac{z}{8}};$$

$$(V): \begin{cases} \frac{x}{3} + \frac{y}{4} + \frac{z}{8} = 1; \\ x = 0, y = 0, z = 0. \end{cases}$$

$$12. I = \int_{\gamma} (x^{4/3} + y^{4/3}) dl, \text{ buyerda } \gamma -$$

astroida: $x^{2/3} + y^{2/3} = a^{2/3}$.

$$13. I = \int_{\gamma} y^2 dx - xy dy, \text{ buyerda } \gamma - A(1;$$

1), B(3; 4) nuqtalarni tutashtiruvchito'g'richiziqke smasi.

4 – variant

$$1. \sum_{n=1}^{\infty} \frac{n}{(2n-1)^2 (2n+1)^2}$$

$$2. \sum_{n=1}^{\infty} \frac{n^3}{3^n};$$

$$3. \sum_{n=1}^{\infty} \left(\frac{1+n}{1+n^2} \right)^2$$

$$4. \sum_{n=1}^{\infty} (-1)^n \cdot \frac{n}{n^2+1}$$

$$5. \sum_{n=1}^{\infty} (nx)^n$$

6. $f(x) = \ln x$ funksiyani $x_0 = 1$ nuqta atrofida Teylor qatoriga yoying.

$$7. \sin 18^\circ, \varepsilon = 0,001$$

$$8. f(x) =$$

$\begin{cases} -x, \text{ agar } -2 \leq x < 0 \text{ bo'lsa,} \\ x, \text{ agar } 0 \leq x \leq 2 \text{ bo'lsa.} \end{cases}$ Ushbu funksiyani Fur'e qatoriga yoying.

$$9. \int_0^1 dy \int_0^{\sqrt{y}} f dx + \int_1^2 dy \int_0^{\sqrt{2-y}} f dx.$$

$$10. \int_0^1 dx \int_{\sqrt{y}}^{2-y} x dx dy$$

$$\iiint_V (3x + 4y) dx dy dz;$$

$$11. (V): \begin{cases} y = x, y = 0, x = 1; \\ z = 3(x^2 + y^2), z = 0. \end{cases}$$

$$12. I = \int_{\gamma} (x - y) dl, \text{ buyerda } \gamma - \text{aylana:}$$

$$x^2 + y^2 = ax.$$

$$13. I = \int_{\gamma} yz dx + zx dy + xy dz, \text{ buyerda } \gamma -$$

vintchizig'ining birinchi o'rami:

$$x = R \cos t, y = R \sin t, z = \frac{at}{2\pi}, 0 \leq t \leq 2\pi.$$

5 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{n(n+3)}$$

$$2. \sum_{n=1}^{\infty} \frac{2^n}{n^2}$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n(\ln n)}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{3n-2}{3n-1}$$

$$5. \sum_{n=1}^{\infty} \frac{(2x-3)^n}{2n-1}$$

6. $f(x) = x^{10} - 3x^5 + 1$ ko'phadni $(x-1)$ ikki hadning darajalari bo'yicha yoying.

$$7. \sin 36^\circ, \varepsilon = 0,001$$

$$8. f(x) =$$

$\begin{cases} -x, \text{ agar } -\pi \leq x < 0 \text{ bo'lsa,} \\ x^2, \text{ agar } 0 \leq x \leq \pi \text{ bo'lsa.} \end{cases}$ Ushbu

funksiyani Fur'e qatoriga yoying.

$$9. \int_{-\sqrt{2}}^{-1} dx \int_{-\sqrt{2-x^2}}^0 fdy + \int_{-1}^0 dx \int_x^0 fdy.$$

$$10. \iint_D \frac{x^2}{y^2} dx dy \quad D: y = -x, y = x^2 \text{ va } y = 1$$

chiziqlar bilan chegaralangan soha.

$$\iiint_V (27x + 54y^2) dx dy dz :$$

$$11. (V): \begin{cases} y = x, y = 0, x = 1; \\ z = \sqrt{xy}, z = 0. \end{cases}$$

$$12. I = \int_{\gamma} (x-y) dl, \text{ buyerda } \gamma \text{ chiziq}$$

$$r^2 = a^2 \cos 2\varphi$$

lemnistikataning o'ngiyaprog'i.

$$13. I = \int_{(1;1;1)}^{(4;4;4)} \frac{xdx + ydy + zdz}{\sqrt{x^2 + y^2 + z^2 - x - y + 2z}}$$

to'g'richiziq kesmasi bo'yicha hisoblansin.

6 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{(3n-1)(3n+2)}$$

$$2. \sum_{n=1}^{\infty} n \left(1 - \frac{1}{n}\right)^{n^2}$$

$$3. \sum_{n=1}^{\infty} \frac{\ln(n+1)}{(n+1)^2}$$

$$4. \sum_{n=1}^{\infty} (-1)^n \cdot \frac{2n}{n+1}$$

$$5. \sum_{n=1}^{\infty} \frac{(x+1)^n}{2^n}$$

6. $f(x) = \frac{1}{x}$ funksiyani $x_0 = 3$ nuqta atrofida Teylor qatoriga yoying.

$$7. \sin 72^\circ, \varepsilon = 0,001$$

8. $f(x) = \sin x$ funksiyani $[0, \pi]$ da kosinuslar bo'yicha Fur'e qatoriga yoying.

$$9. \int_0^{1/\sqrt{2}} dy \int_0^{\arcsin y} f dx + \int_{1/\sqrt{2}}^1 dy \int_0^{\arccos y} f dx.$$

$$10. \iint_D x dx dy \quad D: \text{ sikloidaning bir arkasi.}$$

$$\iiint_V \frac{dx dy dz}{\left(1 + \frac{x}{16} + \frac{y}{8} + \frac{z}{3}\right)^2} :$$

$$11. (V): \begin{cases} \frac{x}{16} + \frac{y}{8} + \frac{z}{3} = 1; \\ x = 0, y = 0, z = 0. \end{cases}$$

$$12. I = \int_{\gamma} (x^2 - z) dl, \text{ buyerda } \gamma \text{ chiziq}$$

$$x = t, y = \frac{\sqrt{3}t^2}{\sqrt{2}}, z = t^3 \text{ egrichiziqning yoyi} \\ (0 \leq t \leq 1).$$

$$13. I = \int_{\gamma} (y-z) dx + (z-x) dy + (x-y) dz,$$

buyerda γ -aylana:

$x^2 + y^2 + z^2 = a^2, y = x \operatorname{tg} \alpha, (0 \leq \alpha \leq 2\pi)$. Ox o'qining musbat qismidan qaraganda ayila nasokat millari harakatiga teskari yo'nalishda o'tilsin.

7 – variant

1. $\sum_{n=1}^{\infty} \frac{5^n + 2^n}{10^n}$
2. $\sum_{n=1}^{\infty} \left(\frac{n+2}{2n+1} \right)^{3n+1}$
3. $\sum_{n=1}^{\infty} n e^{-n^2}$
4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{\ln(n^2+1)}$
5. $\sum_{n=1}^{\infty} n! x^{n-1}$
6. $f(x) = \sqrt{x^3}$ funksiyani $x_0 = 1$ nuqta atrofida Teylor qatoriga yoying.
7. $e^{\frac{1}{2}}, \varepsilon = 0,00001$
8. $f(x) = 1 - \frac{x}{2}$ funksiyani $[0, 2]$ da sinuslar bo'yicha Fur'e qatoriga yoying.
9. $\int_{-2}^{-1} dy \int_0^{\sqrt{2+y}} f dx + \int_{-1}^0 dy \int_0^{\sqrt{-y}} f dx.$
10. $\iint_D y^3 dy dx$ integralni hisoblang buyerda
 $D: y^2 = x, y^2 = 2x, xy = 1$ va $xy = 4$
 chiziqlar bilan chegaralangan soha.
 $\iiint_V (3x^2 + y^2) dx dy dz:$
11. $(V): \begin{cases} z = 10y, & x + y = 1; \\ x = 0, & y = 0, & z = 0. \end{cases}$
12. $I = \int_{\gamma} \sqrt{2y^2 + z^2} dl$, buyerda γ -aylana:
 $\begin{cases} x^2 + y^2 + z^2 = a^2 \\ y = x \end{cases}$.
13. $I = \int_{\gamma} y^2 dx - x^2 dy$, buyerda $\gamma: y = x^2$
 parabolaning $A(0;0), B(2;4)$
 nuqtalar orasidagi yoyi.

8 – variant

1. $\sum_{n=1}^{\infty} \frac{2n+1}{n^2(n+1)^2}$
2. $\sum_{n=1}^{\infty} \left(\arcsin \frac{1}{n} \right)^n$
3. $\sum_{n=1}^{\infty} \frac{1}{\sqrt{n}} \ln \frac{n+1}{n-1}$
4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{\ln(n+1)}$
5. $\sum_{n=1}^{\infty} \frac{n! x^n}{(n+1)^n}$
6. $f(x) = e^x$ funksiyani Makloren qatoriga yoying.
7. $e^{\frac{1}{3}}, \varepsilon = 0,00001$
8. $f(x) = x^3$ funksiyani $[-1; 1]$ da sinuslar bo'yicha Fur'e qatoriga yoying.
9. $\int_0^1 dy \int_{-\sqrt{y}}^0 f dx + \int_1^{e-\ln y} dy \int_{-1}^{-\ln y} f dx.$
10. $\iint \sqrt{x^2 + y^2} dx dy$
 integralni hisoblang buyerda
 $D: x^2 + y^2 = x$ va $x^2 + y^2 = 2x$
 aylanalar bilan chegaralangan soha.
 $\iiint_V (15x + 30z) dx dy dz:$
11. $(V): \begin{cases} z = x^2 + 3y^2, & z = 0; \\ y = x, & y = 0, & x = 1. \end{cases}$
12. $I = \int_{\gamma} x^2 y z dl$, buyerda γ -chiziq
 $x^2 + y^2 = z^2, x^2 + y^2 = 9$
 egrichiziqning (aylana) yoyi.
13. $I = \int_{\gamma} y^2 dx + z^2 dy + x^2 dz$, buyerda γ -
 Vavianachizig'i:
 $x^2 + y^2 + z^2 = a^2, x^2 + y^2 = ax$ ning
 (x,y)
 tekislikdanyuqoridagi qismidir.

9 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{(2n-1)(2n+5)}$$

$$2. \sum_{n=2}^{\infty} \frac{1}{(2n-1) \ln(2n-1)}$$

$$3. \sum_{n=1}^{\infty} \frac{e^{-\sqrt{n}}}{\sqrt{n}}$$

$$4. \sum_{n=1}^{\infty} (-1)^n \cdot \frac{n}{n^2-1}$$

$$5. \sum_{n=1}^{\infty} \frac{(x-1)^n}{2^n}$$

6. $f(x) = 2^x$ funksiyani Makloren qatoriga yoying.

$$7. e^{\frac{1}{4}}, \varepsilon = 0,00001$$

8. $f(x) = \cos x$ funksiyani $[0, \pi]$ da sinuslar bo'yicha Fur'e qatoriga yoying.

$$9. \int_{\sqrt{2}}^{-1} dx \int_0^{\sqrt{2-x^2}} fdy + \int_{-1}^0 dx \int_0^{x^2} fdy.$$

$$10. \iint_D (x^2 + 3y^2 + 2) ds \quad D: x^2 + y^2 = 4$$

$$\iiint_V (4 + 8z^3) dx dy dz :$$

$$11. (V): \begin{cases} y = x, & y = 0, & x = 1; \\ z = \sqrt{xy}, & z = 0. \end{cases}$$

$$I = \int_{\gamma} z dl, \text{ buyerda } \gamma\text{-chiziq}$$

12.

$$x^2 + y^2 = z^2, \quad y^2 = ax$$

egrichiziqning $O(0;0;0)$ nuqtasidan $A(a;a;a\sqrt{2})$ nuqtasigachabo'lganyoyi.

$$I = \int_{\gamma} y^2 dx + x^2 dy, \text{ buyerda } \gamma\text{-chiziq}$$

13.

$a;0)$ nuqtadan $B(a;0)$

gachabo'lganyarimellipsyoyidir:

$$x = a \cos t, \quad y = b \sin t.$$

10 – variant

$$1. \frac{3}{5} + \frac{3}{5} \cdot \frac{1}{3} + \frac{3}{5} \cdot \frac{1}{9} + \frac{3}{5} \cdot \frac{1}{27} + \dots$$

$$2. \sum_{n=1}^{\infty} \frac{2n+3}{3n-2};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln^2 n}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n^3}{2^n}$$

$$5. \sum_{n=0}^{\infty} \frac{(x)^n}{2^n \cdot \sqrt{n+1}}$$

6. $f(x) = \frac{1}{x}$ funksiyani $x_0 = 2$ nuqta atrofida Teylor qatoriga yoying.

$$7. \ln 0,98, \varepsilon = 0,0001$$

$$8. f(x) =$$

$\begin{cases} 1+x, & \text{agar } -1 \leq x < 0 \text{ bo'lsa,} \\ -1, & \text{agar } 0 \leq x \leq 1 \text{ bo'lsa.} \end{cases}$ Ushbu funksiyani Fur'e qatoriga yoying.

$$9. \int_{-2}^{-\sqrt{3}} dx \int_{-\sqrt{4-x^2}}^0 fdy + \int_{-\sqrt{3}}^0 dx \int_{\sqrt{4-x^2}-2}^0 fdy$$

$$10. \iint_D (x^2 + xy + 2y^2) ds \quad D: x=0, y=0 \text{ va } x+y=1$$

chiziqlar bilan chegaralangan soha.

$$\iiint_V (1 + 2x^3) dx dy dz :$$

$$11. (V): \begin{cases} y = 36x, & y = 0, & x = 1; \\ z = \sqrt{xy}, & z = 0. \end{cases}$$

$$I = \int_{\gamma} (2x - 3y) dl, \text{ bu yerda } \gamma \text{ chiziq}$$

12.

$$r = a \sqrt{\cos 2\varphi} \text{ lemnistikataning o'ng yaprog'i.}$$

$$13. I = \int_{\gamma} (y^2 - z^2) dx + 2yz dy - x^2 dz, \text{ buyerda } \gamma$$

egrichiziq $x = t, y = t^2, z = t^3, (0 \leq t \leq 1)$.

11 – variant

$$1. \frac{1}{1 \cdot 2 \cdot 3} + \frac{1}{2 \cdot 3 \cdot 4} + \frac{1}{3 \cdot 4 \cdot 5} + \frac{1}{4 \cdot 5 \cdot 6} + \dots$$

$$2. \sum_{n=1}^{\infty} \frac{1}{\sqrt[3]{n} + 2};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln^5 n}$$

$$4. \sum_{n=1}^{\infty} (-1)^n \cdot \frac{1}{n+1}$$

$$5. \sum_{n=1}^{\infty} \frac{(2x+1)^n}{2n-1}$$

6. $f(x) = \cos \sqrt{x}$ funksiyani Makloren qatoriga yoying.

$$7. \sqrt{27}, \varepsilon = 0,001$$

8. $f(x) = \pi - x$ funksiyani $(-\pi, \pi]$ da Fur'e qatoriga yoying.

$$9. \int_0^{\pi/4} dy \int_0^{\sin y} f dx + \int_{\pi/4}^{\pi/2} dy \int_0^{\cos y} f dx.$$

$$10. \int_0^1 \int_0^2 xy(x+y) dx dy$$

$$\iiint_V (60y + 90z) dx dy dz :$$

$$11. (V) : \begin{cases} y = 4x, y = 0, x = 1; \\ z = x^2 + y^2, z = 0. \end{cases}$$

$$12. I = \int_{AB}^{\gamma} \frac{dl}{\sqrt{x^2 + y^2}}, \text{ buyerda } AB-$$

uchlari $A(0;-2), B(4;0)$

nuqtalardan iborat kesma.

$$13. I = \int_{AB} \cos y dx - \sin x dy, \text{ buyerda } AB-$$

kesma: $A(2;-2), B(-2;2)$.

12 – variant

$$1. \frac{1}{1 \cdot 4} + \frac{1}{4 \cdot 7} + \frac{1}{7 \cdot 10} + \frac{1}{10 \cdot 13} + \dots$$

$$2. \sum_{n=1}^{\infty} \left(1 - \frac{1}{n}\right)^{n^2+1};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln^6 n}$$

$$4. \sum_{n=1}^{\infty} (-1)^n \cdot \frac{1}{n \cdot \ln(n+1)}$$

$$5. \sum_{n=1}^{\infty} \frac{(n+1)^5 x^{2n}}{2n+1}$$

6. $f(x) = \frac{3}{2-x-x^2}$ funksiyani x ning darajalari bo'yicha qatoriga yoying.

$$7. \sqrt{8}, \varepsilon = 0,001$$

8. $f(x) = \frac{x^2}{2} - 1$ funksiyani $[-3; 3]$ da Fur'e qatoriga yoying.

$$9. \int_{-2}^{-1} dx \int_{-(2+x)}^0 f dy + \int_{-1}^0 dx \int_{\sqrt[3]{x}}^0 f dy$$

$$10. \int_0^1 \int_{x^2}^x xy^2 dx dy$$

$$\iiint_V \left(\frac{10}{3}x + \frac{5}{3}\right) dx dy dz :$$

$$11. (V) : \begin{cases} y = 9x, y = 0, x = 1; \\ z = \sqrt{xy}, z = 0. \end{cases}$$

$$I = \int_{\gamma} xy dl, \text{ buyerda } \gamma - \text{ushbu}$$

$$12. x = 0, y = 0, x = 4, y = 2$$

to'g'richiziqlardan tashkil topgan to'rtburchak konturi.

$$13. I = \int_{AB} (x^2 - y^2) dx + xy dy, \text{ buyerda } AB - \text{kesma:}$$

$A(2;2), B(3;4)$.

13 – variant

$$1. \frac{1}{1 \cdot 4} + \frac{1}{2 \cdot 5} + \frac{1}{3 \cdot 6} + \frac{1}{4 \cdot 7} + \dots$$

$$2. \sum_{n=1}^{\infty} \frac{(3n)!}{(n!)^3 2^{3n}};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^{1+\alpha}}, (\alpha > 0)$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n \cdot 2^n}$$

$$5. \sum_{n=1}^{\infty} \frac{(x+1)^n}{(2n-1)!}$$

6. $f(x) = e^{-2x}$ funksiyani Makloren qatoriga yoying.

$$7. \sqrt{24}, \varepsilon = 0,001$$

8. $f(x) = 1 - 2x$ funksiyani $[0, 1]$ da kosinuslar bo'yicha Fur'e qatoriga yoying.

$$9. \int_0^1 dy \int_0^{\sqrt{y}} f dx + \int_1^e dy \int_{\ln y}^1 f dx.$$

$$10. \int_1^e \int_1^y \frac{y}{x} dx dy$$

$$\iiint_V (9 + 18z) dx dy dz :$$

$$11. (V) : \begin{cases} y = 4x, & y = 0, & x = 1; \\ z = \sqrt{xy}, & z = 0. \end{cases}$$

$$12. I = \int_{\gamma} \frac{dl}{x^2 + y^2 + 4}, \text{ buyerda } \gamma -$$

uchlari $O(0;0)$, $A(1;2)$ nuqtalardan iborat kesma.

$$13. I = \int_{AB} (4x + y) dx + (x + 4y) dy, \text{ buyerda}$$

$\vec{AB}$ yoy $y = x^4$ egrichiziqning yoyi: $A(1;1)$ va $B(-1;1)$.

14 – variant

$$1. \frac{2}{3} + \frac{2}{3} \cdot \frac{1}{2} + \frac{2}{3} \cdot \frac{1}{3} + \frac{2}{3} \cdot \frac{1}{4} + \frac{2}{3} \cdot \frac{1}{5} + \dots$$

$$2. \sum_{n=1}^{\infty} \frac{2 + (-1)^n}{n};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^2}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n}$$

$$5. \sum_{n=1}^{\infty} (n+1)x^n$$

6. $f(x) = x \cos 3x$ funksiyani x ning darajalari bo'yicha qatorga yoying.

$$7. sh 0,3, \varepsilon = 0,0001$$

8. $f(x) = x + 1$ funksiyani $(-1; 1]$ yarim intervalda Fur'e qatoriga yoying.

$$9. \int_0^1 dy \int_{-\sqrt{y}}^0 f dx + \int_1^2 dy \int_{-\sqrt{2-y}}^0 f dx.$$

$$10. \int_{-2}^{-1} \int_1^{3+x} \frac{\ln y}{y(x+3)} dx dy$$

$$\iiint_V 25y^2 dx dy dz :$$

$$11. (V) : \begin{cases} x = 15, & 3y + z = 1; \\ x = 0, & y = 0, & z = 0. \end{cases}$$

$$1. 12. I = \int_{\gamma} (x + z) dl, \text{ buyerda } \gamma$$

egrichiziq parametrik tenglamalar bilan berilgan:

$$x = 2at\sqrt{1-t^2}, y = a \cdot \ln(1-t^2), z = 2at^2, 0 \leq t \leq \frac{1}{2}.$$

$$13. I = \int_{AB} y dx - x dy, \text{ buyerda } \vec{AB} \text{ yoy } x^2 + y^2 = 1$$

aylananing $A(-\frac{1}{\sqrt{2}}; -\frac{1}{\sqrt{2}})$ nuqtasidan $B(\frac{1}{\sqrt{2}}; \frac{1}{\sqrt{2}})$ nuqtasigacha soat millari harakati yo'nalishida o'tiladi.

15 – variant

$$1. \frac{1}{1 \cdot 3 \cdot 5} + \frac{1}{3 \cdot 5 \cdot 7} + \frac{1}{5 \cdot 7 \cdot 9} + \frac{1}{7 \cdot 9 \cdot 11} + \dots$$

$$2. \sum_{n=1}^{\infty} \frac{1}{2^n} \cdot \left(1 + \frac{1}{n}\right)^{n^2};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^3}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n}{n^2+1}$$

$$5. \sum_{n=1}^{\infty} \frac{(x)^n}{2^n}$$

$$6. f(x) = \frac{1}{\sqrt{4-x^2}} \text{ funksiyani Makloren qatoriga yoying.}$$

$$7. ch 0,3, \varepsilon = 0,0001$$

$$8. f(x) = \cos^2 x \text{ funksiyani } [-\pi; \pi] \text{ da Fur'e qatoriga yoying.}$$

$$9. \int_0^1 dy \int_{-y}^0 f dx + \int_1^{\sqrt{2}} dy \int_{-\sqrt{2-y^2}}^0 f dx.$$

$$10. \iint_D (x^2 + y^2) dx dy, D: x=0, x=1, y=0, y=x^2$$

$$\iiint_V \frac{dx dy dz}{\left(1 + \frac{x}{2} + \frac{y}{4} + \frac{z}{6}\right)^4} :$$

$$11. (V): \begin{cases} \frac{x}{2} + \frac{y}{4} + \frac{z}{6} = 1; \\ x=0, y=0, z=0. \end{cases}$$

$$12. I = \int_{\gamma} (x+z) dl, \text{ buyerda } \gamma:$$

$$x^2 + y^2 + z^2 = R^2, y = x \text{ aylanayoyining}$$

$$A(0;0;R), B(R/2; R/2; R\sqrt{2})$$

nuqtalar orasidagi kichik qismi.

$$13. I = \int_{\gamma} z dx - x dy + y dz, \text{ buyerda } \gamma \text{ vintchizig'ining}$$

$$A(a;0;0) \text{ nuqtadan } B(a; 0; 2\pi c)$$

gachabo'lgan biroz ramdir:

$$x = a \cos t, y = b \sin t, z = ct, 0 \leq t \leq 2\pi.$$

16 – variant

$$1. \frac{1}{1 \cdot 2} + \frac{1}{2 \cdot 3} + \frac{1}{3 \cdot 4} + \dots + \frac{1}{n(n+1)} + \dots$$

$$2. \sum_{n=2}^{\infty} \frac{1}{n \sqrt{\ln n}};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^4}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n^2}{3^n}$$

$$5. \sum_{n=1}^{\infty} \frac{(x-1)^n}{2^n}$$

$$6. f(x) = \ln(10+x) \text{ funksiyani } x_0 = 1 \text{ nuqta atrofida Teylor qatoriga yoying.}$$

$$7. sh 0,5, \varepsilon = 0,0001$$

$$8. f(x) = \sin^2 x \text{ funksiyani } [-\pi; \pi] \text{ da Fur'e qatoriga yoying.}$$

$$9. \int_0^1 dy \int_0^{y^3} f dx + \int_1^2 dy \int_0^{2-y} f dx.$$

$$10. \iint_D (x+2y) dx dy, D: y=x^2, y=5x-6$$

$$\iiint_V (8y+12z) dx dy dz:$$

$$11. (V): \begin{cases} y=x, y=0, x=1; \\ z=3x^2+2y^2, z=0. \end{cases}$$

$$12. I = \int_{\gamma} (x+z) dl, \text{ buyerda } \gamma \text{ uchlari } O(0;0)$$

$$\text{va } A(4;3)$$

nuqtalarni tutashtiruvchi to'g'richiziq kesmasi.

$$13. I = \int_{\gamma} (x-y) dx + (2x+y) dy, \text{ buyerda } \gamma \text{ uchlari } A(1;1), B(3;3), C(3;-1)$$

$$\text{nuqtalarni tutashtiruvchi uchburchak konturi.}$$

17 – variant

$$1. \frac{1}{1 \cdot 3 \cdot 5} + \frac{1}{3 \cdot 5 \cdot 7} + \dots + \frac{1}{(2n-1)(2n+1)(2n+3)} + \dots$$

$$2. \sum_{n=1}^{\infty} \ln \frac{n^3+1}{n^3};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^5}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n - \ln n}$$

$$5. \sum_{n=1}^{\infty} \frac{(x)^n}{n}$$

6. $f(x) = \arcsin(x)$ funksiyani x ning darajalari bo'yicha qatorga yoying.

$$7. sh 0,37, \varepsilon = 0,0001$$

8. $f(x) = 5x - 4$ funksiyani $[-\pi; \pi]$ da Fur'e qatoriga yoying.

$$9. \int_0^{\sqrt{3}} dx \int_{\sqrt{4-x^2}-2}^0 fdy + \int_{\sqrt{3}}^2 dx \int_{-\sqrt{4-x^2}}^0 fdy$$

$$10. \iint_D e^{x+\cos y} dx dy, D: x=0, x=\pi, y=0, y=\frac{\pi}{2}$$

$$\iiint_V (x+yz) dx dy dz:$$

$$11. (V): \begin{cases} y=x, y=0, x=1; \\ z=30x^2+60y^2, z=0. \end{cases}$$

$$12. I = \int_{\gamma} \frac{dl}{\sqrt{8-x^2-y^2}}, \text{ buyerda } \gamma\text{- uchlar } O(0;0)$$

va $A(2;2)$

nuqtalarni tutashtiruvchito'g'richiziqkesmasi.

$$13. I = \int_{\gamma} ydx - xdy, \text{ buyerda } \gamma\text{- astroida}$$

$$x^{2/3} + y^{2/3} = a^{2/3} \text{ ning } A(a;0) \text{ dan } B(0;a)$$

gachabo'lganyoy.

18 – variant

$$1. 1 + \frac{m-1}{m} + \left(\frac{m-1}{m}\right)^2 + \dots + \left(\frac{m-1}{m}\right)^n + \dots$$

$$2. \sum_{n=1}^{\infty} \left(\frac{2n^2+1}{3n^2+5}\right)^n$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^6}$$

$$\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n-1}{6n+5}$$

$$4. \sum_{n=1}^{\infty} \frac{(x)^n}{n}$$

6. $f(x) = \ln(1+x)$ funksiyani $x_0 = 1$ nuqta atrofida Teylor qatoriga yoying.

$$7. th 0,3, \varepsilon = 0,0001$$

8. $f(x) = \begin{cases} -4, \text{ agar } -\pi \leq x < 0 \text{ bo'lsa,} \\ 4, \text{ agar } 0 \leq x \leq \pi \text{ bo'lsa.} \end{cases}$ Ushbu funksiyani Fur'e qatoriga yoying.

$$9. \int_{-2}^{-1} dy \int_{-(2+y)}^0 fdx + \int_{-1}^0 dy \int_{\sqrt[3]{y}}^0 fdx$$

$$10.$$

$$\iint_D x \sin(x+y) dx dy, D: x=0, x=\pi, y=0, y=\frac{\pi}{2}$$

$$\iiint_V \frac{dx dy dz}{\left(1 + \frac{x}{6} + \frac{y}{4} + \frac{z}{16}\right)^2}:$$

$$11. (V): \begin{cases} \frac{x}{6} + \frac{y}{4} + \frac{z}{16} = 1; \\ x=0, y=0, z=0. \end{cases}$$

$$12. I = \int_{\gamma} y dl, \text{ buyerda } \gamma: y^2 = 2\sqrt{3}x \text{ parabolaning}$$

$$x^2 = 2\sqrt{3}y \text{ parabola bilan kesilgan bo'lagi.}$$

$$13. I = \int_{\gamma} xdx + ydy + zdz, \text{ buyerda } \gamma: A(a;0;0)$$

dan $B(a; 0; 2\pi b)$ gachabo'lgan

$x = a \cos t, y = a \sin t, z = bt, 0 \leq t \leq 2\pi$ vintchizig'ining o'rami.

19 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{n^2 + 6n + 5}$

2. $\sum_{n=1}^{\infty} \frac{n}{2^n}$

3. $\sum_{n=2}^{\infty} \frac{1}{n^{\alpha} \ln^{\beta} n}$

4. $\sum_{n=1}^{\infty} \frac{\sin n\alpha}{n^3}$

5. $\sum_{n=1}^{\infty} (nx)^n$

6. $f(x) = \frac{5}{6+x-x^2}$ funksiyani
Makloren qatoriga yoying.

7. $th\ 0,3, \varepsilon = 0,0001$

8. $f(x) = |x| - 2$ funksiyani
 $[-\pi; \pi]$ da Fur'e qatoriga yoying.

9. $\int_0^1 dx \int_0^{x^2} fdy + \int_1^{\sqrt{2}} dx \int_0^{\sqrt{2-x^2}} fdy$

10. $\iint_D \frac{x^2}{y^2} dx dy, D: xy = 1, y = x, x = 2$

$\iiint_V y^2 dx dy dz :$

11. $(V): \begin{cases} z = 10(3x + y), y + x = 1; \\ x = 0, y = 0, z = 0. \end{cases}$

12. $I = \int_{\gamma} \sqrt{x^2 + y^2} dl$, buyerda γ :

$x^2 + y^2 = 4x$ aylanayoyi.

13. $I = \int_{\gamma} \frac{1}{y} dx + \frac{1}{z} dy + \frac{1}{x} dz$, buyerda γ :

$A(1;1;1)$ va $B(2;4;8)$

dano'tganto'g' richiziqkesmasi.

20 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{n^2 + 4n}$

2. $\sum_{n=1}^{\infty} \left(\frac{2n^2 + 1}{n^2 + 1} \right)^{n^2}$

3. $\sum_{n=2}^{\infty} \frac{1}{n^2 \ln^2 n}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{\sqrt{n+1}}$

5. $\sum_{n=1}^{\infty} \frac{(2x-3)^n}{2n-1}$

6. $f(x) = \frac{1-e^x}{x}$ funksiyani x ning darajalari bo'yicha
qatoriga yoying.

7. $cth\ 0,3, \varepsilon = 0,0001$

8. $f(x) = x^2 - x$ funksiyani $[-2; 2]$ da Fur'e
qatoriga yoying.

9. $\int_{-2}^2 dx \int_{\frac{x^2}{4}}^1 fdy$

$\iint_D e^x y dx dy, D: x = 0, x = 2, y = 1, y = e^x$

10.

$\iiint_V (5x + \frac{3}{2}z) dx dy dz :$

11. $(V): \begin{cases} y = x, y = 0, x = 1; \\ z = x^2 + 15y^2, z = 0. \end{cases}$

12. $I = \int_{\gamma} xy dl$, buyerda γ : $3x + 4y = 12$

to'g' richiziqning koordinata o'qlariga asoslangan kesmasi.

13. $I = \int_{\gamma} e^{y-z} dx + e^{z-x} dy + e^{x-y} dz$, buyerda γ : $O(0;0;0)$

bilan $A(1;3;5)$ ni birlashtiruvchi kesma.

21 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{n^2 + 4n + 3}$$

$$2. \sum_{n=1}^{\infty} \left(\frac{2n+1}{3n-2} \right)^{n^2}$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n^2 \ln^3 n}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{3^n}{n^3}$$

$$5. \sum_{n=1}^{\infty} \frac{(2x-3)^n}{2n-1}$$

6. $f(x) = \frac{6}{8+2x-x^2}$ funksiyani $x_0 = 1$ nuqta atrofida Teylor qatoriga yoying.

$$7. \arcsin 0,4, \varepsilon = 0,0001$$

8. $f(x) = 2x$ funksiyani $(0; 1)$ intervalda Fur'e qatoriga yoying.

$$9. \int_0^1 dx \int_{-2\sqrt{x}}^{2\sqrt{x}} f dy$$

$$10. \iint_D (x^2 + y^2) dx dy, D: x=0, x=1, y=0, y=x^2$$

$$\iiint_V \frac{dx dy dz}{\left(1 + \frac{x}{8} + \frac{y}{3} + \frac{z}{5}\right)^2} :$$

$$11. (V): \begin{cases} \frac{x}{8} + \frac{y}{3} + \frac{z}{5} = 1; \\ x=0, y=0, z=0. \end{cases}$$

$$12. I = \int_{\gamma} xy dl, \text{ buyerda } \gamma: 4x + 3y = 12$$

to'g'richiziqning koordinata o'qlar orasidagi kesmasi.

$$13. I = \int_{\gamma} (y+z)dx + (2+x)dy + (x+y)dz, \text{ buyerda}$$

γ -yoy: $x^2 + y^2 + z^2 = 25$ sferadagi $M(3; 4; 0)$ bilan $A(0; 0; 5)$ nibirlashtiruvchikatta aylananing eng qisqayoyi.

22 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{n^2 + n - 12}$$

$$2. \sum_{n=1}^{\infty} \frac{2^{n+1}}{n^n}$$

$$3. \sum_{n=1}^{\infty} \frac{1}{\sqrt{n+1}}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n+1}{n^2 + n + 1}$$

$$5. \sum_{n=1}^{\infty} \frac{n! x^n}{(n+1)^n}$$

6. $f(x) = \ln(1 + x - 12x^2)$ funksiyani Makloren qatoriga yoying.

$$7. \arcsin 0,6, \varepsilon = 0,0001$$

8. $f(x) = \begin{cases} -2, & \text{agar } -\pi \leq x < 0 \text{ bo'lsa,} \\ 1, & \text{agar } 0 \leq x \leq \pi \text{ bo'lsa.} \end{cases}$ Ushbu funksiyani Fur'e qatoriga yoying.

$$9. \int_0^4 dx \int_{3x^2}^{12x} f dy$$

$$10. \iiint_V x dx dy dz, V: x=0, y=0, y=3, z=0, x+z=2$$

$$11. \iiint_V 10x^2 dx dy dz :$$

$$(V): \begin{cases} y=8, & 3x+5z=1; \\ x=0, & y=0, z=0. \end{cases}$$

$$12. I = \int_{\gamma} xy(x+y) dl, \text{ buyerda } \gamma: x^2 + y^2 = R^2$$

aylananing yuqoriyoyi.

$$13. I = \int_{\gamma} \frac{y}{x} dx + x dy, \text{ buyerda } \gamma: y = \ln x$$

egrichiziqning $A(0; 1)$ va $B(e; 1)$ nuqtalar orasidagi yoyi.

23 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{9n^2 - 3n - 2}$$

$$2. \sum_{n=1}^{\infty} \left(\frac{n}{10n+5} \right)^{n^2}$$

$$3. \sum_{n=1}^{\infty} \frac{1}{\sqrt{3n+4}}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{\sqrt{5n+3}}$$

$$5. \sum_{n=1}^{\infty} \frac{(x)^n}{(2n-1)!}$$

6. $f(x) = 2x \cdot \cos^2 \frac{x}{2} - x$ funksiyani x ning darajalari bo'yicha qatorga yoying.

$$7. \arcsin 0,9, \varepsilon = 0,0001$$

$$8. f(x) = \pi - 2x, T = 2\pi, [-\pi; \pi].$$

$f(x)$ funksiyani $[0; \pi]$ kesmada juft davom ettirib Fur'e qatoriga yoying.

$$9. \int_0^{\frac{\pi}{2}} dx \int_0^{\sin x} f dy$$

10.

$$\iiint_V xyz dx dy dz, V: x=0, y=0, z=0, x+z+y=1$$

$$\iiint_V 25(y^2 + x) dx dy dz :$$

$$11. (V): \begin{cases} z = x + 3y, x + 2y = 1; \\ x = 0, y = 0, z = 0. \end{cases}$$

$$12. I = \int_{\gamma} \sqrt{x^2 + y^2} dl, \text{ buyerda } \gamma: r = a(1 + \cos \varphi)$$

kardioidayoyi.

$$13. I = \int_{\gamma} (ye^x + 2x) dx + e^x dy, \text{ buyerda } \gamma: y = xe^2$$

egrichiziqning $A(0; 0)$ va $B(1; e)$ nuqtalarorasi dagiyoyi.

24 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{9n^2 + 9n + 20}$$

$$2. \sum_{n=1}^{\infty} \frac{2n+1}{3^n (n-1)!}$$

$$3. \sum_{n=1}^{\infty} n^3 e^{-n^4}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n^3 + 4}$$

$$5. \sum_{n=1}^{\infty} \frac{(n+1)^5 x^{2n}}{2n+1}$$

6. $f(x) = \sqrt[3]{8 - x^3}$ funksiyani Makloren qatoriga yoying.

$$7. \arccos 0,4, \varepsilon = 0,0001$$

$$8. (x) = \begin{cases} x, \text{ agar } 0 \leq x < 1 \text{ bo'lsa,} \\ 2, \text{ agar } 1 \leq x \leq 2 \text{ bo'lsa.} \end{cases} T = 4, [0; 4].$$

$f(x)$ funksiyani $[0; 2]$ kesmada juft davom ettirib Fur'e qatoriga yoying.

$$9. \int_0^1 dx \int_x^{\sqrt{2-x^2}} f dy$$

$$10. \iiint_V (x^2 + y^2) dx dy dz, V: z = 2, z = \frac{x^2 + y^2}{2}$$

$$\iiint_V \frac{dx dy dz}{1 + \frac{x}{3} + \frac{y}{2} + \frac{z}{8}} :$$

$$11. (V): \begin{cases} \frac{x}{3} + \frac{y}{2} + \frac{z}{8} = 1; \\ x = 0, y = 0, z = 0. \end{cases}$$

$$12. I = \int_{\gamma} y^2 dl, \text{ bu yerda } \gamma:$$

$x = a(t - \sin t), y = a(1 - \cos t), (0 \leq t \leq 2\pi)$ sikloidaning bir arkasi.

$$13. I = \int_{\gamma} y^2 dx + x^2 dy, \text{ buyerda } \gamma: \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

ellipsning $A(0; b)$ va $B(a; 0)$ nuqtalarorasi dagiyoyi.

25 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{4n^2 + 4n + 3}$

2. $\sum_{n=1}^{\infty} \frac{(n!)^2}{2^{n^2}}$

3. $\sum_{n=1}^{\infty} n^4 e^{-n^5}$

4. $\sum_{n=1}^{\infty} \frac{\cos 2n\alpha}{n^2 + 1}$

5. $\sum_{n=1}^{\infty} \frac{(x+1)^n}{(2n-1)!}$

6. $f(x) = \ln(10+x)$ funksiyani $x_0 = 0$ nuqta atrofida Teylor qatoriga yoying.

7. $\arccos 0,3, \varepsilon = 0,0001$

8. $f(x) = 3x - 2$ funksiyani $(-1; 1)$ intervalda Fur'e qatoriga yoying.

9. $\int_0^3 dx \int_{\sqrt{2x-x^2}}^{\sqrt{2x}} fdy$

10.

$\iiint_V (x^2 + y^2) dx dy dz, V: x^2 + y^2 = x, z = 0, z^2 = 2x$

$\iiint_V 4xy dx dy dz:$

11. $(V): \begin{cases} y = 6x, y = 0, x = 1; \\ z = 3(x^2 + 2y^2), z = 0. \end{cases}$

12. $I = \int_{\gamma} (x^2 + y^2 + z^2) dl$, buyerda γ :

$x = \cos t, y = \sin t, z = \sqrt{3}t, (0 \leq t \leq 2\pi)$

vintchizig'ining birinchi o'rami.

13. $I = \int_{\gamma} x dy - y dx$, buyerda $\gamma: x^2 + y^2 = R^2$ aylananing yoyi.

26 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{9n^2 + 21n + 10}$

2. $\sum_{n=1}^{\infty} \frac{10^n \cdot n!}{(2n+1)!}$

3. $\sum_{n=1}^{\infty} n^2 e^{-n^3}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n+3}{n^2-9}$

5. $\sum_{n=0}^{\infty} \frac{(x)^n}{2^n \cdot \sqrt{n+1}}$

6. $f(x) = x \cos 3x$ funksiyani $x_0 = 3$ ning darajalari bo'yicha qatoriga yoying.

7. $\arctg 3, \varepsilon = 0,0001$

8. $f(x) = x^2 - 1$ funksiyani $(-1; 1)$ intervalda Fur'e qatoriga yoying.

9. $\int_0^1 dy \int_{-4y-4}^{-8y^3} f dx$

10.

$\iiint_V \frac{dx dy dz}{\sqrt{x^2 + y^2}}, V: x^2 + y^2 = 4y, y + z = 4, z = 0$

$\iiint_V (7x^2 + 2y) dx dy dz:$

11. $(V): \begin{cases} y = 20x, y = 0, x = 1; \\ z = \sqrt{3xy}, z = 0. \end{cases}$

12. $I = \int_{\gamma} \frac{x}{3y+z} dl$, buyerda γ :

$x = \frac{t^2}{\sqrt{2}}, y = \frac{t^3}{3}, z = t$ chiziqning $A(0;0;0)$ va

$B(\sqrt{2}; \frac{2\sqrt{2}}{3}; \sqrt{2})$ nuqtalar orasidagi yoyi.

13. $I = \int_{\gamma} x dy - y dx$, buyerda $\gamma: y = x^2, x = y^2$ parabolalar orasidagi grichiziq yoyi.

27 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{n^2 + 9n + 20}$

2. $\sum_{n=1}^{\infty} \frac{n^2 + 1}{(n+2)!}$

3. $\sum_{n=3}^{\infty} \frac{1}{n \ln n \ln(\ln n)}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n-1}{n^2 - 2n + 1}$

5. $\sum_{n=0}^{\infty} \frac{(x-2)^n}{2^n \cdot \sqrt{n+1}}$

6. $f(x) = x \sin x$ funksiyani $x_0 = 1$ ning darajalari bo'yicha qatorga yoying.

7. $\sqrt[5]{1,1}, \varepsilon = 0,00001$

8. $f(x) = \begin{cases} -x^2, & \text{agar } -\pi \leq x < 0 \text{ bo'lsa,} \\ 1-x, & \text{agar } 0 \leq x \leq \pi \text{ bo'lsa.} \end{cases}$
Ushbu funksiyani Fur'e qatoriga yoying.

9. $\int_1^3 dy \int_0^{2y} f dx$

$x=1, y=x, y=2x, z=x^2+y^2, z=x^2+2y^2$

10.

$$\iiint_V \frac{dx dy dz}{\left(1 + \frac{x}{15} + \frac{y}{8} + \frac{z}{4}\right)^2} :$$

11. $(V) : \begin{cases} \frac{x}{15} + \frac{y}{8} + \frac{z}{4} = 1; \\ x=0, y=0, z=0. \end{cases}$

$I = \int_{\gamma} \frac{1}{\sqrt{x^2 + y^2 + z^2}} dl$, bu yerda $\gamma: A(1; 2)$

12.

va $B(3; 6)$ nuqtalarni tutashtiruvchi to'g'ri chiziq kesmasi.

13. $I = \int_{\gamma} x dy - y dx$, buyerda $\gamma:$

$x=4\cos^3 t, y=4\sin^3 t$ astroidayoyi.

28 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{49n^2 + 35n - 6}$

2. $\sum_{n=1}^{\infty} \frac{(n+3)!}{n^n}$

3. $\sum_{n=3}^{\infty} \frac{1}{n \ln(\ln n)}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n \cdot 3^n}$

5. $\sum_{n=1}^{\infty} \frac{(2x+1)^n}{2n-1}$

6. $f(x) = \frac{1}{\sqrt{9-x^2}}$ funksiyani x ning darajalari bo'yicha qatorga yoying.

7. $\sqrt[3]{2}, \varepsilon = 0,00001$

8. $f(x) = \begin{cases} 1, & \text{agar } -1 \leq x < 0 \text{ bo'lsa,} \\ -x^2, & \text{agar } 0 \leq x \leq 1 \text{ bo'lsa.} \end{cases}$
Ushbu funksiyani Fur'e qatoriga yoying.

9. $\int_0^2 dx \int_{\sqrt{2x-x^2}}^{2\sqrt{x}} f dy$

10. $x=0, y=0, x+2y+z=6$

$$\iiint_V x^2 dx dy dz :$$

11. $(V) : \begin{cases} y=3, & x+z=1; \\ x=0, & y=0, & z=0. \end{cases}$

12. $I = \int_{\gamma} y dl$, bu yerda $\gamma: y^2=4x, x^2=4y$

parabolalar orasidagi egri chiziq yoyi.

13. $I = \int_{\gamma} x dx + y dy + (x-y+1) dz$, buyerda $\gamma:$

$A(1; 1; 1)$ va $B(2; 3; 4)$

nuqtalarni tutashtiruvchi to'g'ri chiziq.

29 – variant

$$1. \frac{1}{1 \cdot 2 \cdot 3} + \frac{1}{2 \cdot 3 \cdot 4} + \frac{1}{3 \cdot 4 \cdot 5} + \frac{1}{4 \cdot 5 \cdot 6} + \dots$$

$$2. \sum_{n=1}^{\infty} \frac{1}{\sqrt[3]{n+2}};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln^5 n}$$

$$4. \sum_{n=1}^{\infty} (-1)^n \cdot \frac{1}{n+1}$$

$$5. \sum_{n=1}^{\infty} \frac{(2x+1)^n}{2n-1}$$

6. $f(x) = \cos \sqrt{x}$ funksiyani Makloren qatoriga yoying.

$$7. \sqrt{27}, \varepsilon = 0,001$$

8. $f(x) = \pi - x$ funksiyani $(-\pi, \pi]$ da Fur'e qatoriga yoying.

$$9. \int_0^{\pi/4} dy \int_0^{\sin y} f dx + \int_{\pi/4}^{\pi/2} dy \int_0^{\cos y} f dx.$$

$$10. \int_0^1 \int_0^2 xy(x+y) dx dy$$

$$\iiint_V (60y + 90z) dx dy dz:$$

$$11. (V): \begin{cases} y = 4x, y = 0, x = 1; \\ z = x^2 + y^2, z = 0. \end{cases}$$

$$12. I = \int_{AB}^{\gamma} \frac{dl}{\sqrt{x^2 + y^2}}, \text{ buyerda } AB\text{-uchlari } A(0;-$$

2), $B(4;0)$ nuqtalardan iborat kesma.

13. $I = \int_{AB} \cos y dx - \sin x dy$, buyerda AB -kesma: $A(2;-2)$, $B(-2;2)$.

30 – variant

$$1. \frac{1}{1 \cdot 4} + \frac{1}{4 \cdot 7} + \frac{1}{7 \cdot 10} + \frac{1}{10 \cdot 13} + \dots$$

$$2. \sum_{n=1}^{\infty} \left(1 - \frac{1}{n}\right)^{n^2+1};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln^6 n}$$

$$4. \sum_{n=1}^{\infty} (-1)^n \cdot \frac{1}{n \cdot \ln(n+1)}$$

$$5. \sum_{n=1}^{\infty} \frac{(n+1)^5 x^{2n}}{2n+1}$$

6. $f(x) = \frac{3}{2-x-x^2}$ funksiyani x ning darajalari bo'yicha qatoriga yoying.

$$7. \sqrt{8}, \varepsilon = 0,001$$

8. $f(x) = \frac{x^2}{2} - 1$ funksiyani $[-3; 3]$ da Fur'e qatoriga yoying.

$$9. \int_{-2}^{-1} dx \int_{-(2+x)}^0 f dy + \int_{-1}^0 dx \int_{\sqrt[3]{x}}^0 f dy$$

$$10. \int_0^1 \int_{x^2}^x xy^2 dx dy$$

$$\iiint_V \left(\frac{10}{3}x + \frac{5}{3}\right) dx dy dz:$$

$$11. (V): \begin{cases} y = 9x, y = 0, x = 1; \\ z = \sqrt{xy}, z = 0. \end{cases}$$

$$I = \int_{\gamma} xy dl, \text{ buyerda } \gamma\text{-ushbu}$$

$$12. x = 0, y = 0, x = 4, y = 2$$

to'g'richiziqlardan tashkil topgan to'rtburchak konturi.

13. $I = \int_{AB} (x^2 - y^2) dx + xy dy$, buyerda AB -kesma: $A(2;2)$, $B(3;4)$.

31 – variant

$$1. \frac{1}{1 \cdot 4} + \frac{1}{2 \cdot 5} + \frac{1}{3 \cdot 6} + \frac{1}{4 \cdot 7} + \dots$$

$$2. \sum_{n=1}^{\infty} \frac{(3n)!}{(n!)^3 2^{3n}};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^{1+\alpha}}, (\alpha > 0)$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n \cdot 2^n}$$

$$5. \sum_{n=1}^{\infty} \frac{(x+1)^n}{(2n-1)!}$$

6. $f(x) = e^{-2x}$ funksiyani Makloren qatoriga yoying.

$$7. \sqrt{24}, \varepsilon = 0,001$$

8. $f(x) = 1 - 2x$ funksiyani $[0, 1]$ da kosinuslar bo'yicha Fur'e qatoriga yoying.

$$9. \int_0^1 dy \int_0^{\sqrt{y}} f dx + \int_1^e dy \int_{\ln y}^1 f dx$$

$$10. \int_1^e \int_1^y \frac{y}{x} dx dy$$

$$\iiint_V (9 + 18z) dx dy dz :$$

$$11. (V) : \begin{cases} y = 4x, & y = 0, & x = 1; \\ z = \sqrt{xy}, & z = 0. \end{cases}$$

$$12. I = \int_{\gamma} \frac{dl}{x^2 + y^2 + 4}, \text{ buyerda } \gamma -$$

uchlari $O(0;0)$, $A(1;2)$

nuqtalardan iborat kesma.

$$13. I = \int_{AB} (4x + y) dx + (x + 4y) dy, \text{ buyerda } A \bar{B}$$

yoy $y = x^4$ egrichiziqning yoyi: $A(1;1)$ va $B(-1;1)$.

32 – variant

$$1. \frac{2}{3} + \frac{2}{3} \cdot \frac{1}{2} + \frac{2}{3} \cdot \frac{1}{4} + \frac{2}{3} \cdot \frac{1}{8} + \dots$$

$$2. \sum_{n=1}^{\infty} \frac{2 + (-1)^n}{n};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^2}$$

$$\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n}$$

$$4. \sum_{n=1}^{\infty} (n+1)x^n$$

6. $f(x) = x \cos 3x$ funksiyani x ning darajalari bo'yicha qatorga yoying.

$$7. sh 0,3, \varepsilon = 0,0001$$

8. $f(x) = x + 1$ funksiyani $(-1; 1]$ yarim intervalda Fur'e qatoriga yoying.

$$9. \int_0^1 dy \int_{-\sqrt{y}}^0 f dx + \int_1^2 dy \int_{-\sqrt{2-y}}^0 f dx$$

$$10. \int_{-2}^{-1} \int_1^{3+x} \frac{\ln y}{y(x+3)} dx dy$$

$$\iiint_V 25y^2 dx dy dz :$$

$$11. (V) : \begin{cases} x = 15, & 3y + z = 1; \\ x = 0, & y = 0, & z = 0. \end{cases}$$

$$2. 12. I = \int_{\gamma} (x + z) dl, \text{ buyerda } \gamma$$

egrichiziq parametrik tenglamalar bilan berilgan:

$$x = 2at\sqrt{1-t^2}, y = a \cdot \ln(1-t^2), z = 2at^2, 0 \leq t \leq 1$$

$$13. I = \int_{A\bar{B}} y dx - x dy, \text{ buyerda } A \bar{B} \text{ yoy}$$

$$x^2 + y^2 = 1 \text{ aylananing } A(-\frac{1}{\sqrt{2}}; -\frac{1}{\sqrt{2}}) \text{ nuqtasidan}$$

$$B(\frac{1}{\sqrt{2}}; \frac{1}{\sqrt{2}})$$

nuqtasigacha soat millari harakati yo'nalishida o'tiladi

33 – variant

1. $\frac{1}{1 \cdot 3 \cdot 5} + \frac{1}{3 \cdot 5 \cdot 7} + \frac{1}{5 \cdot 7 \cdot 9} + \frac{1}{7 \cdot 9 \cdot 11} + \dots$
2. $\sum_{n=1}^{\infty} \frac{1}{2^n} \cdot \left(1 + \frac{1}{n}\right)^{n^2};$
3. $\sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^3}$
4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n}{n^2+1}$
5. $\sum_{n=1}^{\infty} \frac{(x)^n}{2^n}$
6. $f(x) = \frac{1}{\sqrt{4-x^2}}$ funksiyani Makloren qatoriga yoying.
7. $ch\ 0,3, \varepsilon = 0,0001$
8. $f(x) = \cos^2 x$ funksiyani $[-\pi; \pi]$ da Fur'e qatoriga yoying.
9. $\int_0^1 dy \int_{-y}^0 f dx + \int_1^{\sqrt{2}} dy \int_{-\sqrt{2-y^2}}^0 f dx.$
10. $\iint_D (x^2 + y^2) dx dy, D: x=0, x=1, y=0, y=x^2$
- $$\iiint_V \frac{dx dy dz}{\left(1 + \frac{x}{2} + \frac{y}{4} + \frac{z}{6}\right)^4};$$
11. $(V): \begin{cases} \frac{x}{2} + \frac{y}{4} + \frac{z}{6} = 1; \\ x=0, y=0, z=0. \end{cases}$
12. $I = \int_{\gamma} (x+z) dl$, buyerda γ :
 $x^2 + y^2 + z^2 = R^2, y=x$ aylanayoyining
 $A(0;0;R), B(R/2; R/2; R\sqrt{2})$
 nuqtalar orasidagi kichik qismi.
13. $I = \int_{\gamma} z dx - x dy + y dz$, buyerda γ
 vintchizig'ining $A(a;0;0)$ nuqtadan $B(a; 0; 2\pi c)$
 gachabo'lgan biroz ramdir:
 $x = a \cos t, y = b \sin t, z = ct, 0 \leq t \leq 2\pi.$

34 – variant

1. $\frac{1}{1 \cdot 2} + \frac{1}{2 \cdot 3} + \frac{1}{3 \cdot 4} + \dots + \frac{1}{n(n+1)} + \dots$
2. $\sum_{n=2}^{\infty} \frac{1}{n \sqrt{\ln n}};$
3. $\sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^4}$
4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n^2}{3^n}$
5. $\sum_{n=1}^{\infty} \frac{(x-1)^n}{2^n}$
6. $f(x) = \ln(10+x)$ funksiyani $x_0 = 1$ nuqta atrofida Teylor qatoriga yoying.
7. $sh\ 0,5, \varepsilon = 0,0001$
8. $f(x) = \sin^2 x$ funksiyani $[-\pi; \pi]$ da Fur'e qatoriga yoying.
9. $\int_0^1 dy \int_0^{y^3} f dx + \int_1^2 dy \int_0^{2-y} f dx$
10. $\iint_D (x+2y) dx dy, D: y=x^2, y=5x-6$

$$\iiint_V (8y+12z) dx dy dz;$$
11. $(V): \begin{cases} y=x, y=0, x=1; \\ z=3x^2+2y^2, z=0. \end{cases}$
12. $I = \int_{\gamma} (x+z) dl$, bu yerda γ - uchlari
 $O(0;0)$ va $A(4;3)$ nuqtalarni
 tutashtiruvchi to'g'ri chiziqli kesmasi.
13. $I = \int_{\gamma} (x-y) dx + (2x+y) dy$, bu yerda γ
 - uchlari $A(1;1), B(3;3), C(3;-1)$
 nuqtalarni tutashtiruvchi uchburchak
 konturi.

35 – variant

$$1. \frac{1}{1 \cdot 3 \cdot 5} + \frac{1}{3 \cdot 5 \cdot 7} + \dots + \frac{1}{(2n-1)(2n+1)(2n+3)} + \dots$$

$$2. \sum_{n=1}^{\infty} \ln \frac{n^3 + 1}{n^3};$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^5}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n - \ln n}$$

$$5. \sum_{n=1}^{\infty} \frac{(x)^n}{n}$$

6. $f(x) = \arcsin(x)$ funksiyani x ning darajalari bo'yicha qatorga yoying.

$$7. sh\ 0,37, \varepsilon = 0,0001$$

8. $f(x) = 5x - 4$ funksiyani $[-\pi; \pi]$ da Fur'e qatoriga yoying.

$$9. \int_0^{\sqrt{3}} dx \int_{\sqrt{4-x^2}-2}^0 fdy + \int_{\sqrt{3}}^2 dx \int_{-\sqrt{4-x^2}}^0 fdy$$

$$10. \iint_D e^{x+\cos y} dx dy, D: x=0, x=\pi, y=0, y=\frac{\pi}{2}$$

$$\iiint_V (x+yz) dx dy dz:$$

$$11. (V): \begin{cases} y=x, y=0, x=1; \\ z=30x^2+60y^2, z=0. \end{cases}$$

$$12. I = \int_{\gamma} \frac{dl}{\sqrt{8-x^2-y^2}}, \text{ bu yerda } \gamma\text{- uchlari}$$

$O(0;0)$ va $A(2;2)$ nuqtalarni tutashtiruvchi to'g'ri chiziqli kesmasi.

$$13. I = \int_{\gamma} y dx - x dy, \text{ bu yerda } \gamma\text{- astroida}$$

$x^{2/3} + y^{2/3} = a^{2/3}$ ning $A(a;0)$ dan $B(0;a)$ gacha bo'lgan yoy.

36 – variant

$$1. 1 + \frac{m-1}{m} + \left(\frac{m-1}{m}\right)^2 + \dots + \left(\frac{m-1}{m}\right)^n + \dots$$

$$2. \sum_{n=1}^{\infty} \left(\frac{2n^2+1}{3n^2+5}\right)^n$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^6}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n-1}{6n+5}$$

$$5. \sum_{n=1}^{\infty} \frac{(x)^n}{n}$$

6. $f(x) = \ln(1+x)$ funksiyani $x_0 = 1$ nuqta atrofida Teylor qatoriga yoying.

$$7. th\ 0,3, \varepsilon = 0,0001$$

8. $f(x) = \begin{cases} -4, & \text{agar } -\pi \leq x < 0 \text{ bo'lsa,} \\ 4, & \text{agar } 0 \leq x \leq \pi \text{ bo'lsa.} \end{cases}$ Ushbu funksiyani Fur'e qatoriga yoying.

$$9. \int_{-2}^{-1} dy \int_{-(2+y)}^0 f dx + \int_{-1}^0 dy \int_{\sqrt[3]{y}}^0 f dx$$

$$10. \iint_D x \sin(x+y) dx dy, D: x=0, x=\pi, y=0, y=\frac{\pi}{2}$$

$$\iiint_V \frac{dx dy dz}{\left(1 + \frac{x}{6} + \frac{y}{4} + \frac{z}{16}\right)^2}:$$

$$11. (V): \begin{cases} \frac{x}{6} + \frac{y}{4} + \frac{z}{16} = 1; \\ x=0, y=0, z=0. \end{cases}$$

$$12. I = \int_{\gamma} y dl, \text{ bu yerda } \gamma: y^2 = 2\sqrt{3}x \text{ parabolaning}$$

$x^2 = 2\sqrt{3}y$ parabola bilan kesilgan bo'lagi.

$$13. I = \int_{\gamma} x dx + y dy + z dz, \text{ bu yerda } \gamma: A(a;0;0) \text{ dan}$$

$B(a; 0; 2\pi b)$ gacha bo'lgan

$x = a \cos t, y = a \sin t, z = bt, 0 \leq t \leq 2\pi$ vint chizig'ining o'rami.

37 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{n^2 + 6n + 5}$

2. $\sum_{n=1}^{\infty} \frac{n}{2^n}$

3. $\sum_{n=2}^{\infty} \frac{1}{n^{\alpha} \ln^{\beta} n}$

4. $\sum_{n=1}^{\infty} \frac{\sin n\alpha}{n^3}$

5. $\sum_{n=1}^{\infty} (nx)^n$

6. $f(x) = \frac{5}{6+x-x^2}$ funksiyani Makloren qatoriga yoying.

7. $\text{th } 0,3, \varepsilon = 0,0001$

8. $f(x) = |x| - 2$ funksiyani $[-\pi; \pi]$ da Fur'e qatoriga yoying.

9. $\int_0^1 dx \int_0^{x^2} fdy + \int_1^{\sqrt{2}} dx \int_0^{\sqrt{2-x^2}} fdy$

10. $\iint_D \frac{x^2}{y^2} dx dy, D: xy=1, y=x, x=2$

$\iiint_V y^2 dx dy dz :$

11. $(V): \begin{cases} z=10(3x+y), y+x=1; \\ x=0, y=0, z=0. \end{cases}$

12. $I = \int_{\gamma} \sqrt{x^2 + y^2} dl$, bu yerda γ :

$x^2 + y^2 = 4x$ aylana yoyi.

13. $I = \int_{\gamma} \frac{1}{y} dx + \frac{1}{z} dy + \frac{1}{x} dz$, bu yerda γ :

$A(1;1;1)$ va $B(2; 4;8)$ dan o'tgan to'g'ri chiziq kesmasi.

38 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{n^2 + 4n}$

2. $\sum_{n=1}^{\infty} \left(\frac{2n^2 + 1}{n^2 + 1} \right)^{n^2}$

3. $\sum_{n=2}^{\infty} \frac{1}{n^2 \ln^2 n}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{\sqrt{n+1}}$

5. $\sum_{n=1}^{\infty} \frac{(2x-3)^n}{2n-1}$

6. $f(x) = \frac{1-e^x}{x}$ funksiyani x ning darajalari bo'yicha qatorga yoying.

7. $\text{cth } 0,3, \varepsilon = 0,0001$

8. $f(x) = x^2 - x$ funksiyani $[-2; 2]$ da Fur'e qatoriga yoying.

9. $\int_{-2}^2 dx \int_{\frac{x^2}{4}}^1 fdy$

$\iint_D e^x y dx dy, D: x=0, x=2, y=1, y=e^x$

10.

$\iiint_V (5x + \frac{3}{2}z) dx dy dz :$

11. $(V): \begin{cases} y=x, y=0, x=1; \\ z=x^2+15y^2, z=0. \end{cases}$

12. $I = \int_{\gamma} xy dl$, bu yerda γ : $3x + 4y = 12$ to'g'ri chiziqning koordinata o'qlari orasidagi kesmasi.

13. $I = \int_{\gamma} e^{y-z} dx + e^{z-x} dy + e^{x-y} dz$, bu yerda γ :

$O(0;0;0)$ bilan $A(1;3;5)$ ni birlashtiruvchi kesma.

39 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{n^2 + 4n + 3}$$

$$2. \sum_{n=1}^{\infty} \left(\frac{2n+1}{3n-2} \right)^{n^2}$$

$$3. \sum_{n=2}^{\infty} \frac{1}{n^2 \ln^3 n}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{3^n}{n^3}$$

$$5. \sum_{n=1}^{\infty} \frac{(2x-3)^n}{2n-1}$$

6. $f(x) = \frac{6}{8+2x-x^2}$ funksiyani $x_0 = 1$ nuqta atrofida Teylor qatoriga yoying.

$$7. \arcsin 0,4, \varepsilon = 0,0001$$

8. $f(x) = 2x$ funksiyani $(0; 1)$ intervalda Fur'e qatoriga yoying.

$$9. \int_0^1 dx \int_{-2\sqrt{x}}^{2\sqrt{x}} f dy$$

$$10. \iint_D (x^2 + y^2) dx dy, D: x=0, x=1, y=0, y=x^2$$

$$\iiint_V \frac{dx dy dz}{\left(1 + \frac{x}{8} + \frac{y}{3} + \frac{z}{5}\right)^2} :$$

$$11. (V): \begin{cases} \frac{x}{8} + \frac{y}{3} + \frac{z}{5} = 1; \\ x=0, y=0, z=0. \end{cases}$$

12. $I = \int_{\gamma} xy dl$, bu yerda $\gamma: 4x + 3y = 12$ to'g'ri chiziqning koordinata o'qlari orasidagi kesmasi.

$$13. I = \int_{\gamma} (y+z)dx + (2+x)dy + (x+y)dz, \text{ bu}$$

yerda γ -yoy: $x^2 + y^2 + z^2 = 25$ sferadagi $M(3; 4; 0)$ bilan $A(0; 0; 5)$ ni birlashtiruvchi katta aylananing eng qisqa yoyi.

40 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{n^2 + n - 12}$$

$$2. \sum_{n=1}^{\infty} \frac{2^{n+1}}{n^n}$$

$$3. \sum_{n=1}^{\infty} \frac{1}{\sqrt{n+1}}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n+1}{n^2 + n + 1}$$

$$5. \sum_{n=1}^{\infty} \frac{n! x^n}{(n+1)^n}$$

6. $f(x) = \ln(1 + x - 12x^2)$ funksiyani Makloren qatoriga yoying.

$$7. \arcsin 0,6, \varepsilon = 0,0001$$

$$8. f(x) = \begin{cases} -2, & \text{agar } -\pi \leq x < 0 \text{ bo'lsa,} \\ 1, & \text{agar } 0 \leq x \leq \pi \text{ bo'lsa.} \end{cases}$$

Ushbu funksiyani Fur'e qatoriga yoying.

$$9. \int_0^4 dx \int_{3x^2}^{12x} f dy$$

$$10.$$

$$\iiint_V x dx dy dz, V: x=0, y=0, y=3, z=0, x+z=2$$

$$11.$$

$$\iiint_V 10x^2 dx dy dz :$$

$$(V): \begin{cases} y=8, & 3x+5z=1; \\ x=0, & y=0, z=0. \end{cases}$$

$$12. I = \int_{\gamma} xy(x+y) dl, \text{ bu yerda } \gamma: x^2 + y^2 = R^2$$

aylananing yuqori yoyi.

$$13. I = \int_{\gamma} \frac{y}{x} dx + x dy, \text{ bu yerda } \gamma: y = \ln x \text{ egri}$$

chiziqning $A(0; 1)$ va $B(e; 1)$ nuqtalar orasidagi yoyi.

41 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{9n^2 - 3n - 2}$$

$$2. \sum_{n=1}^{\infty} \left(\frac{n}{10n+5} \right)^{n^2}$$

$$3. \sum_{n=1}^{\infty} \frac{1}{\sqrt{3n+4}}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{\sqrt{5n+3}}$$

$$5. \sum_{n=1}^{\infty} \frac{(x)^n}{(2n-1)!}$$

6. $f(x) = 2x \cdot \cos^2 \frac{x}{2} - x$ funksiyani x ning darajalari bo'yicha qatorga yoying.

$$7. \arcsin 0,9, \varepsilon = 0,0001$$

8. $f(x) = \pi - 2x, T = 2\pi, [-\pi; \pi]$.
 $f(x)$ funksiyani $[0; \pi]$ kesmada juft davom ettirib Fur'e qatoriga yoying.

$$9. \int_0^{\frac{\pi}{2}} dx \int_0^{\sin x} f dy$$

$$10. \iiint_V xyz dx dy dz, V: x=0, y=0, z=0, x+z+y=1$$

$$\iiint_V 25(y^2 + x) dx dy dz :$$

$$11. (V): \begin{cases} z = x + 3y, x + 2y = 1; \\ x = 0, y = 0, z = 0. \end{cases}$$

$$12. I = \int_{\gamma} \sqrt{x^2 + y^2} dl, \text{ bu yerda } \gamma:$$

$r = a(1 + \cos \varphi)$ kardioda yoyi.

$$13. I = \int_{\gamma} (ye^x + 2x) dx + e^x dy, \text{ bu yerda } \gamma:$$

$y = xe^2$ egri chiziqning $A(0;0)$ va $B(1;e)$ nuqtalar orasidagi yoyi.

42 – variant

$$1. \sum_{n=1}^{\infty} \frac{1}{9n^2 + 9n + 20}$$

$$2. \sum_{n=1}^{\infty} \frac{2n+1}{3^n (n-1)!}$$

$$3. \sum_{n=1}^{\infty} n^3 e^{-n^4}$$

$$4. \sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n^3 + 4}$$

$$5. \sum_{n=1}^{\infty} \frac{(n+1)^5 x^{2n}}{2n+1}$$

6. $f(x) = \sqrt[3]{8 - x^3}$ funksiyani Makloren qatoriga yoying.

$$7. \arccos 0,4, \varepsilon = 0,0001$$

8. $(x) = \begin{cases} x, \text{ agar } 0 \leq x < 1 \text{ bo'lsa,} \\ 2, \text{ agar } 1 \leq x \leq 2 \text{ bo'lsa.} \end{cases} T = 4,$
 $[0; 4]$. $f(x)$ funksiyani $[0; 2]$ kesmada juft davom ettirib Fur'e qatoriga yoying.

$$9. \int_0^1 dx \int_x^{\sqrt{2-x^2}} f dy$$

$$10. \iiint_V (x^2 + y^2) dx dy dz, V: z=2, z = \frac{x^2 + y^2}{2}$$

$$\iiint_V \frac{dx dy dz}{1 + \frac{x}{3} + \frac{y}{2} + \frac{z}{8}} :$$

$$11. (V): \begin{cases} \frac{x}{3} + \frac{y}{2} + \frac{z}{8} = 1; \\ x = 0, y = 0, z = 0. \end{cases}$$

$$12. I = \int_{\gamma} y^2 dl, \text{ bu yerda } \gamma:$$

$x = a(t - \sin t), y = a(1 - \cos t), (0 \leq t \leq 2\pi)$ sikloidaning bir arkasi.

$$13. I = \int_{\gamma} y^2 dx + x^2 dy, \text{ bu yerda } \gamma: \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

ellipsning $A(0;b)$ va $B(a;0)$ nuqtalar orasidagi yoyi.

43 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{4n^2 + 4n + 3}$

2. $\sum_{n=1}^{\infty} \frac{(n!)^2}{2^{n^2}}$

3. $\sum_{n=1}^{\infty} n^4 e^{-n^5}$

4. $\sum_{n=1}^{\infty} \frac{\cos 2n\alpha}{n^2 + 1}$

5. $\sum_{n=1}^{\infty} \frac{(x+1)^n}{(2n-1)!}$

6. $f(x) = \ln(10+x)$ funksiyani $x_0 = 0$ nuqta atrofida Teylor qatoriga yoying.

7. $\arccos 0,3, \varepsilon = 0,0001$

8. $f(x) = 3x - 2$ funksiyani $(-1; 1)$ intervalda Fur'e qatoriga yoying.

9. $\int_0^3 dx \int_{\sqrt{2x-x^2}}^{\sqrt{2x}} fdy$

10.

$\iiint_V (x^2 + y^2) dx dy dz, V: x^2 + y^2 = x, z = 0, z^2 = 2x$
 $\iiint_V 4xy dx dy dz:$

11. $(V): \begin{cases} y = 6x, y = 0, x = 1; \\ z = 3(x^2 + 2y^2), z = 0. \end{cases}$

12. $I = \int_{\gamma} (x^2 + y^2 + z^2) dl$, bu yerda $\gamma:$

$x = \cos t, y = \sin t, z = \sqrt{3}t, (0 \leq t \leq 2\pi)$ vint chizig'ining birinchi o'rami.

13. $I = \int_{\gamma} x dy - y dx$, bu yerda $\gamma: x^2 + y^2 = R^2$ aylananing yoyi.

44 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{9n^2 + 2 \ln n + 10}$

2. $\sum_{n=1}^{\infty} \frac{10^n \cdot n!}{(2n+1)!}$

3. $\sum_{n=1}^{\infty} n^2 e^{-n^3}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n+3}{n^2-9}$

5. $\sum_{n=0}^{\infty} \frac{(x)^n}{2^{n \cdot \sqrt{n+1}}}$

6. $f(x) = x \cos 3x$ funksiyani $x_0 = 3$ ning darajalari bo'yicha qatoriga yoying.

7. $\arctg 3, \varepsilon = 0,0001$

8. $f(x) = x^2 - 1$ funksiyani $(-1; 1)$ intervalda Fur'e qatoriga yoying.

9. $\int_0^1 dy \int_{-4y-4}^{-8y^3} f dx$

10. $\iiint_V \frac{dx dy dz}{\sqrt{x^2 + y^2}}, V: x^2 + y^2 = 4y, y + z = 4, z = 0$

$\iiint_V (7x^2 + 2y) dx dy dz:$

11. $(V): \begin{cases} y = 20x, y = 0, x = 1; \\ z = \sqrt{3xy}, z = 0. \end{cases}$

12. $I = \int_{\gamma} \frac{x}{3y+z} dl$, bu yerda $\gamma:$

$x = \frac{t^2}{\sqrt{2}}, y = \frac{t^3}{3}, z = t$ chiziqning $A(0;0;0)$ va

$B(\sqrt{2}; \frac{2\sqrt{2}}{3}; \sqrt{2})$ nuqtalar orasidagi yoyi.

13. $I = \int_{\gamma} x dy - y dx$, bu yerda $\gamma: y = x^2, x = y^2$ parabolalar orasidagi egri chiziq yoyi.

45 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{n^2 + 9n + 20}$

2. $\sum_{n=1}^{\infty} \frac{n^2 + 1}{(n+2)!}$

3. $\sum_{n=3}^{\infty} \frac{1}{n \ln n \ln(\ln n)}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n-1}{n^2 - 2n + 1}$

5. $\sum_{n=0}^{\infty} \frac{(x-2)^n}{2^n \cdot \sqrt{n+1}}$

6. $f(x) = x \sin x$ funksiyani $x_0 = 1$ ning darajalari bo'yicha qatorga yoying.

7. $\sqrt[5]{1}, \varepsilon = 0,00001$

8. $f(x) = \begin{cases} -x^2, & \text{agar } -\pi \leq x < 0 \text{ bo'lsa,} \\ 1-x, & \text{agar } 0 \leq x \leq \pi \text{ bo'lsa.} \end{cases}$

Ushbu funksiyani Fur'e qatoriga yoying.

9. $\int_1^3 dy \int_0^{2y} f dx$

$x=1, y=x, y=2x, z=x^2+y^2, z=x^2+2y^2$

10.

$$\iiint_V \frac{dx dy dz}{\left(1 + \frac{x}{15} + \frac{y}{8} + \frac{z}{4}\right)^2} :$$

11. $(V) : \begin{cases} \frac{x}{15} + \frac{y}{8} + \frac{z}{4} = 1; \\ x=0, y=0, z=0. \end{cases}$

$I = \int_{\gamma} \frac{1}{\sqrt{x^2 + y^2 + z^2}} dl$, bu yerda γ : $A(1;2)$ va

12.

$B(3;6)$ nuqtalarni tutashtiruvchi to'g'ri chiziq kesmasi.

13. $I = \int_{\gamma} x dy - y dx$, bu yerda γ :

$x=4\cos^3 t, y=4\sin^3 t$ astroida yoyi.

46 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{49n^2 + 35n - 6}$

2. $\sum_{n=1}^{\infty} \frac{(n+3)!}{n^n}$

3. $\sum_{n=3}^{\infty} \frac{1}{n \ln(\ln n)}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n \cdot 3^n}$

5. $\sum_{n=1}^{\infty} \frac{(2x+1)^n}{2n-1}$

6. $f(x) = \frac{1}{\sqrt{9-x^2}}$ funksiyani x ning darajalari bo'yicha qatorga yoying.

7. $\sqrt[3]{2}, \varepsilon = 0,00001$

8. $f(x) = \begin{cases} 1, & \text{agar } -1 \leq x < 0 \text{ bo'lsa,} \\ -x^2, & \text{agar } 0 \leq x \leq 1 \text{ bo'lsa.} \end{cases}$

Ushbu funksiyani Fur'e qatoriga yoying.

9. $\int_0^2 dx \int_{\sqrt{2x-x^2}}^{2\sqrt{x}} f dy$

10. $x=0, y=0, x+2y+z=6$

$$\iiint_V x^2 dx dy dz :$$

11. $(V) : \begin{cases} y=3, & x+z=1; \\ x=0, & y=0, z=0. \end{cases}$

12. $I = \int_{\gamma} y dl$, bu yerda γ : $y^2=4x, x^2=4y$

parabolalar orasidagi egri chiziq yoyi.

13. $I = \int_{\gamma} x dx + y dy + (x-y+1) dz$, bu yerda γ :

$A(1;1;1)$ va $B(2;3;4)$ nuqtalarni tutashtiruvchi to'g'ri chiziq.

47 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{n^2 + 6n + 5}$

2. $\sum_{n=1}^{\infty} \frac{n}{2^n}$

3. $\sum_{n=2}^{\infty} \frac{1}{n^{\alpha} \ln^{\beta} n}$

4. $\sum_{n=1}^{\infty} \frac{\sin n\alpha}{n^3}$

5. $\sum_{n=1}^{\infty} (nx)^n$

6. $f(x) = \frac{5}{6+x-x^2}$ funksiyani Makloren qatoriga yoying.

7. $th\ 0,3, \varepsilon = 0,0001$

8. $f(x) = |x| - 2$ funksiyani $[-\pi; \pi]$ da Fur'e qatoriga yoying.

9. $\int_0^1 dx \int_0^{x^2} fdy + \int_1^{\sqrt{2}} dx \int_0^{\sqrt{2-x^2}} fdy$

10. $\iint_D \frac{x^2}{y^2} dx dy, D: xy=1, y=x, x=2$

$\iiint_V y^2 dx dy dz :$

11. $(V): \begin{cases} z=10(3x+y), y+x=1; \\ x=0, y=0, z=0. \end{cases}$

12. $I = \int_{\gamma} \sqrt{x^2 + y^2} dl$, bu yerda γ :

$x^2 + y^2 = 4x$ aylana yoyi.

13. $I = \int_{\gamma} \frac{1}{y} dx + \frac{1}{z} dy + \frac{1}{x} dz$, bu yerda γ :

$A(1;1;1)$ va $B(2; 4;8)$ dan o'tgan to'g'ri chiziq kesmasi.

48 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{n^2 + 4n}$

2. $\sum_{n=1}^{\infty} \left(\frac{2n^2 + 1}{n^2 + 1} \right)^{n^2}$

3. $\sum_{n=2}^{\infty} \frac{1}{n^2 \ln^2 n}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{\sqrt{n+1}}$

5. $\sum_{n=1}^{\infty} \frac{(2x-3)^n}{2n-1}$

6. $f(x) = \frac{1-e^x}{x}$ funksiyani x ning darajalari bo'yicha qatoriga yoying.

7. $cth\ 0,3, \varepsilon = 0,0001$

8. $f(x) = x^2 - x$ funksiyani $[-2; 2]$ da Fur'e qatoriga yoying.

9. $\int_{-2}^2 dx \int_{\frac{x^2}{4}}^1 fdy$

$\iint_D e^x y dx dy, D: x=0, x=2, y=1, y=e^x$

10.

$\iiint_V (5x + \frac{3}{2}z) dx dy dz :$

11. $(V): \begin{cases} y=x, y=0, x=1; \\ z=x^2+15y^2, z=0. \end{cases}$

12. $I = \int_{\gamma} xy dl$, bu yerda γ : $3x+4y=12$ to'g'ri chiziqning koordinata o'qlari orasidagi kesmasi.

13. $I = \int_{\gamma} e^{y-z} dx + e^{z-x} dy + e^{x-y} dz$, bu yerda γ :

$O(0;0;0)$ bilan $A(1;3;5)$ ni birlashtiruvchi kesma.

49 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{n^2 + 4n + 3}$
2. $\sum_{n=1}^{\infty} \left(\frac{2n+1}{3n-2} \right)^{n^2}$
3. $\sum_{n=2}^{\infty} \frac{1}{n^2 \ln^3 n}$
4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{3^n}{n^3}$
5. $\sum_{n=1}^{\infty} \frac{(2x-3)^n}{2n-1}$
6. $f(x) = \frac{6}{8+2x-x^2}$ funksiyani $x_0 = 1$ nuqta atrofida Teylor qatoriga yoying.
7. $\arcsin 0,4, \varepsilon = 0,0001$
8. $f(x) = 2x$ funksiyani $(0; 1)$ intervalda Fur'e qatoriga yoying.
9. $\int_0^1 dx \int_{-2\sqrt{x}}^{2\sqrt{x}} fdy$
10. $\iint_D (x^2 + y^2) dx dy, D: x=0, x=1, y=0, y=x^2$
11. $\iiint_V \frac{dx dy dz}{\left(1 + \frac{x}{8} + \frac{y}{3} + \frac{z}{5}\right)^2} :$
 $(V): \begin{cases} \frac{x}{8} + \frac{y}{3} + \frac{z}{5} = 1; \\ x=0, y=0, z=0. \end{cases}$
12. $I = \int_{\gamma} xy dl$, bu yerda $\gamma: 4x + 3y = 12$ to'g'ri chiziqning koordinata o'qlari orasidagi kesmasi.
13. $I = \int_{\gamma} (y+z)dx + (2+x)dy + (x+y)dz$, bu yerda γ -yoy: $x^2 + y^2 + z^2 = 25$ sferadagi $M(3;4;0)$ bilan $A(0;0;5)$ ni birlashtiruvchi katta aylananing eng qisqa yoyi.

50 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{n^2 + n - 12}$
2. $\sum_{n=1}^{\infty} \frac{2^{n+1}}{n^n}$
3. $\sum_{n=1}^{\infty} \frac{1}{\sqrt{n+1}}$
4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n+1}{n^2 + n + 1}$
5. $\sum_{n=1}^{\infty} \frac{n! x^n}{(n+1)^n}$
6. $f(x) = \ln(1 + x - 12x^2)$ funksiyani Makloren qatoriga yoying.
7. $\arcsin 0,6, \varepsilon = 0,0001$
8. $f(x) = \begin{cases} -2, & \text{agar } -\pi \leq x < 0 \text{ bo'lsa,} \\ 1, & \text{agar } 0 \leq x \leq \pi \text{ bo'lsa.} \end{cases}$
Ushbu funksiyani Fur'e qatoriga yoying.
9. $\int_0^4 dx \int_{3x^2}^{12x} fdy$
10. $\iiint_V x dx dy dz, V: x=0, y=0, y=3, z=0, x+z=2$
11. $\iiint_V 10x^2 dx dy dz :$
 $(V): \begin{cases} y=8, & 3x+5z=1; \\ x=0, & y=0, z=0. \end{cases}$
12. $I = \int_{\gamma} xy(x+y) dl$, bu yerda $\gamma: x^2 + y^2 = R^2$ aylananing yuqori yoyi.
13. $I = \int_{\gamma} \frac{y}{x} dx + x dy$, bu yerda $\gamma: y = \ln x$ egri chiziqning $A(0;1)$ va $B(e;1)$ nuqtalar orasidagi yoyi.

51– variant

1. $\sum_{n=1}^{\infty} \frac{1}{9n^2 - 3n - 2}$

2. $\sum_{n=1}^{\infty} \left(\frac{n}{10n+5} \right)^{n^2}$

3. $\sum_{n=1}^{\infty} \frac{1}{\sqrt{3n+4}}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{\sqrt{5n+3}}$

5. $\sum_{n=1}^{\infty} \frac{(x)^n}{(2n-1)!}$

6. $f(x) = 2x \cdot \cos^2 \frac{x}{2} - x$ funksiyani x ning darajalari bo'yicha qatorga yoying.

7. $\arcsin 0,9, \varepsilon = 0,0001$

8. $f(x) = \pi - 2x, T = 2\pi, [-\pi; \pi]$.
 $f(x)$ funksiyani $[0; \pi]$ kesmada juft davom ettirib Fur'e qatoriga yoying.

9. $\int_0^{\frac{\pi}{2}} dx \int_0^{\sin x} f dy$

10. $\iiint_V xyz dx dy dz, V: x=0, y=0, z=0, x+z+y=1$

$\iiint_V 25(y^2 + x) dx dy dz :$

11. $(V): \begin{cases} z = x + 3y, x + 2y = 1; \\ x = 0, y = 0, z = 0. \end{cases}$

12. $I = \int_{\gamma} \sqrt{x^2 + y^2} dl,$ bu yerda $\gamma:$

$r = a(1 + \cos \varphi)$ kardioida yoyi.

13. $I = \int_{\gamma} (ye^x + 2x) dx + e^x dy,$ bu yerda $\gamma:$

$y = xe^2$ egri chiziqning $A(0;0)$ va $B(1;e)$ nuqtalar orasidagi yoyi.

52– variant

1. $\sum_{n=1}^{\infty} \frac{1}{9n^2 + 9n + 20}$

2. $\sum_{n=1}^{\infty} \frac{2n+1}{3^n (n-1)!}$

3. $\sum_{n=1}^{\infty} n^3 e^{-n^4}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n^3+4}$

5. $\sum_{n=1}^{\infty} \frac{(n+1)^5 x^{2n}}{2n+1}$

6. $f(x) = \sqrt[3]{8 - x^3}$ funksiyani Makloren qatoriga yoying.

7. $\arccos 0,4, \varepsilon = 0,0001$

8. $(x) = \begin{cases} x, \text{ agar } 0 \leq x < 1 \text{ bo'lsa,} \\ 2, \text{ agar } 1 \leq x \leq 2 \text{ bo'lsa.} \end{cases} T = 4, [0; 4].$
 $f(x)$ funksiyani $[0; 2]$ kesmada juft davom ettirib Fur'e qatoriga yoying.

9. $\int_0^1 dx \int_x^{\sqrt{2-x^2}} f dy$

10. $\iiint_V (x^2 + y^2) dx dy dz, V: z=2, z = \frac{x^2 + y^2}{2}$

$\iiint_V \frac{dx dy dz}{1 + \frac{x}{3} + \frac{y}{2} + \frac{z}{8}} :$

11. $(V): \begin{cases} \frac{x}{3} + \frac{y}{2} + \frac{z}{8} = 1; \\ x = 0, y = 0, z = 0. \end{cases}$

12. $I = \int_{\gamma} y^2 dl,$ bu yerda $\gamma:$

$x = a(t - \sin t), y = a(1 - \cos t), (0 \leq t \leq 2\pi)$ sikloidaning bir arkasi.

13. $I = \int_{\gamma} y^2 dx + x^2 dy,$ bu yerda $\gamma: \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ ellipsning $A(0;b)$ va $B(a;0)$ nuqtalar orasidagi yoyi.

53 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{4n^2 + 4n + 3}$

2. $\sum_{n=1}^{\infty} \frac{(n!)^2}{2^{n^2}}$

3. $\sum_{n=1}^{\infty} n^4 e^{-n^5}$

4. $\sum_{n=1}^{\infty} \frac{\cos 2n\alpha}{n^2 + 1}$

5. $\sum_{n=1}^{\infty} \frac{(x+1)^n}{(2n-1)!}$

6. $f(x) = \ln(10 + x)$ funksiyani $x_0 = 0$ nuqta atrofida Teylor qatoriga yoying.

7. $\arccos 0,3, \varepsilon = 0,0001$

8. $f(x) = 3x - 2$ funksiyani $(-1; 1)$ intervalda Fur'e qatoriga yoying.

9. $\int_0^3 dx \int_{\sqrt{2x-x^2}}^{\sqrt{2x}} fdy$

10.

$\iiint_V (x^2 + y^2) dx dy dz, V: x^2 + y^2 = x, z = 0, z^2 = 2x$

$\iiint_V 4xy dx dy dz:$

11. $(V): \begin{cases} y = 6x, y = 0, x = 1; \\ z = 3(x^2 + 2y^2), z = 0. \end{cases}$

12. $I = \int_{\gamma} (x^2 + y^2 + z^2) dl$, bu yerda $\gamma:$

$x = \cos t, y = \sin t, z = \sqrt{3}t, (0 \leq t \leq 2\pi)$ vint chizig'ining birinchi o'rami.

13. $I = \int_{\gamma} x dy - y dx$, bu yerda $\gamma: x^2 + y^2 = R^2$ aylananing yoyi.

54 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{9n^2 + 21n + 10}$

2. $\sum_{n=1}^{\infty} \frac{10^n \cdot n!}{(2n+1)!}$

3. $\sum_{n=1}^{\infty} n^2 e^{-n^3}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n+3}{n^2-9}$

5. $\sum_{n=0}^{\infty} \frac{(x)^n}{2^{n \cdot \sqrt{n+1}}}$

6. $f(x) = x \cos 3x$ funksiyani $x_0 = 3$ ning darajalari bo'yicha qatoriga yoying.

7. $\arctg 3, \varepsilon = 0,0001$

8. $f(x) = x^2 - 1$ funksiyani $(-1; 1)$ intervalda Fur'e qatoriga yoying.

9. $\int_0^1 dy \int_{-4y-4}^{-8y^3} f dx$

10. $\iiint_V \frac{dx dy dz}{\sqrt{x^2 + y^2}}, V: x^2 + y^2 = 4y, y + z = 4, z = 0$

$\iiint_V (7x^2 + 2y) dx dy dz:$

11. $(V): \begin{cases} y = 20x, y = 0, x = 1; \\ z = \sqrt{3xy}, z = 0. \end{cases}$

12. $I = \int_{\gamma} \frac{x}{3y+z} dl$, bu yerda $\gamma:$

$x = \frac{t^2}{\sqrt{2}}, y = \frac{t^3}{3}, z = t$ chiziqning $A(0;0;0)$ va

$B(\sqrt{2}; \frac{2\sqrt{2}}{3}; \sqrt{2})$ nuqtalar orasidagi yoyi.

13. $I = \int_{\gamma} x dy - y dx$, bu yerda $\gamma: y = x^2, x = y^2$ parabolalar orasidagi egri chiziq yoyi.

55 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{n^2 + 9n + 20}$

2. $\sum_{n=1}^{\infty} \frac{n^2 + 1}{(n+2)!}$

3. $\sum_{n=3}^{\infty} \frac{1}{n \ln n \ln(\ln n)}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{n-1}{n^2 - 2n + 1}$

5. $\sum_{n=0}^{\infty} \frac{(x-2)^n}{2^{n \cdot \sqrt{n+1}}}$

6. $f(x) = x \sin x$ funksiyani $x_0 = 1$ ning darajalari bo'yicha qatorga yoying.

7. $\sqrt[5]{1,1}, \varepsilon = 0,00001$

8. $f(x) = \begin{cases} -x^2, & \text{agar } -\pi \leq x < 0 \text{ bo'lsa,} \\ 1-x, & \text{agar } 0 \leq x \leq \pi \text{ bo'lsa.} \end{cases}$

Ushbu funksiyani Fur'e qatoriga yoying.

9. $\int_1^3 dy \int_0^{2y} f dx$

$x=1, y=x, y=2x, z=x^2+y^2, z=x^2+2y^2$

10.

$$\iiint_V \frac{dx dy dz}{\left(1 + \frac{x}{15} + \frac{y}{8} + \frac{z}{4}\right)^2} :$$

11. $(V) : \begin{cases} \frac{x}{15} + \frac{y}{8} + \frac{z}{4} = 1; \\ x=0, y=0, z=0. \end{cases}$

$I = \int_{\gamma} \frac{1}{\sqrt{x^2 + y^2 + z^2}} dl$, bu yerda $\gamma: A(1;2)$

12.

va $B(3;6)$ nuqtalarni tutashtiruvchi to'g'ri chiziq kesmasi.

13. $I = \int_{\gamma} x dy - y dx$, bu yerda $\gamma:$

$x=4\cos^3 t, y=4\sin^3 t$ astroida yoyi.

56 – variant

1. $\sum_{n=1}^{\infty} \frac{1}{49n^2 + 35n - 6}$

2. $\sum_{n=1}^{\infty} \frac{(n+3)!}{n^n}$

3. $\sum_{n=3}^{\infty} \frac{1}{n \ln(\ln n)}$

4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n \cdot 3^n}$

5. $\sum_{n=1}^{\infty} \frac{(2x+1)^n}{2n-1}$

6. $f(x) = \frac{1}{\sqrt{9-x^2}}$ funksiyani x ning darajalari bo'yicha qatorga yoying.

7. $\sqrt[3]{2}, \varepsilon = 0,00001$

8. $f(x) = \begin{cases} 1, & \text{agar } -1 \leq x < 0 \text{ bo'lsa,} \\ -x^2, & \text{agar } 0 \leq x \leq 1 \text{ bo'lsa.} \end{cases}$

Ushbu funksiyani Fur'e qatoriga yoying.

9. $\int_0^2 dx \int_{\sqrt{2x-x^2}}^{2\sqrt{x}} f dy$

10. $x=0, y=0, x+2y+z=6$

$$\iiint_V x^2 dx dy dz :$$

11. $(V) : \begin{cases} y=3, & x+z=1; \\ x=0, & y=0, z=0. \end{cases}$

12. $I = \int_{\gamma} y dl$, bu yerda $\gamma: y^2=4x, x^2=4y$

parabolalar orasidagi egri chiziq yoyi.

13. $I = \int_{\gamma} x dx + y dy + (x-y+1) dz$, bu yerda $\gamma:$

$A(1;1;1)$ va $B(2;3;4)$ nuqtalarni tutashtiruvchi to'g'ri chiziq.

57 – variant

1. $\frac{1}{1 \cdot 2 \cdot 3} + \frac{1}{2 \cdot 3 \cdot 4} + \frac{1}{3 \cdot 4 \cdot 5} + \frac{1}{4 \cdot 5 \cdot 6} + \dots$
2. $\sum_{n=1}^{\infty} \frac{1}{\sqrt[3]{n+2}};$
3. $\sum_{n=2}^{\infty} \frac{1}{n \ln^5 n}$
4. $\sum_{n=1}^{\infty} (-1)^n \cdot \frac{1}{n+1}$
5. $\sum_{n=1}^{\infty} \frac{(2x+1)^n}{2n-1}$
6. $f(x) = \cos \sqrt{x}$ funksiyani Makloren qatoriga yoying.
7. $\sqrt{27}, \varepsilon = 0,001$
8. $f(x) = \pi - x$ funksiyani $(-\pi, \pi]$ da Fur'e qatoriga yoying.
9. $\int_0^{\pi/4} dy \int_0^{\sin y} f dx + \int_{\pi/4}^{\pi/2} dy \int_0^{\cos y} f dx.$
10. $\int_0^1 \int_0^2 xy(x+y) dx dy$
 $\iiint_V (60y + 90z) dx dy dz:$
11. $(V): \begin{cases} y = 4x, y = 0, x = 1; \\ z = x^2 + y^2, z = 0. \end{cases}$
12. $I = \int_{AB}^{\gamma} \frac{dl}{\sqrt{x^2 + y^2}},$ bu yerda AB -uchlari $A(0;-2), B(4;0)$ nuqtalardan iborat kesma.
13. $I = \int_{AB} \cos y dx - \sin x dy,$ bu yerda AB -kesma: $A(2;-2), B(-2;2).$

58 – variant

1. $\frac{1}{1 \cdot 4} + \frac{1}{4 \cdot 7} + \frac{1}{7 \cdot 10} + \frac{1}{10 \cdot 13} + \dots$
2. $\sum_{n=1}^{\infty} \left(1 - \frac{1}{n}\right)^{n^2+1};$
3. $\sum_{n=2}^{\infty} \frac{1}{n \ln^6 n}$
4. $\sum_{n=1}^{\infty} (-1)^n \cdot \frac{1}{n \cdot \ln(n+1)}$
5. $\sum_{n=1}^{\infty} \frac{(n+1)^5 x^{2n}}{2n+1}$
6. $f(x) = \frac{3}{2-x-x^2}$ funksiyani x ning darajalari bo'yicha qatoriga yoying.
7. $\sqrt{8}, \varepsilon = 0,001$
8. $f(x) = \frac{x^2}{2} - 1$ funksiyani $[-3; 3]$ da Fur'e qatoriga yoying.
9. $\int_{-2}^{-1} dx \int_{-(2+x)}^0 f dy + \int_{-1}^0 dx \int_{\sqrt[3]{x}}^0 f dy$
10. $\int_0^1 \int_{x^2}^x xy^2 dx dy$
 $\iiint_V \left(\frac{10}{3}x + \frac{5}{3}\right) dx dy dz:$
11. $(V): \begin{cases} y = 9x, y = 0, x = 1; \\ z = \sqrt{xy}, z = 0. \end{cases}$
 $I = \int_{\gamma} xy dl,$ bu yerda γ -ushbu
12. $x = 0, y = 0, x = 4, y = 2$ to'g'ri chiziqlardan tashkil topgan to'rtburchak konturi.
13. $I = \int_{AB} (x^2 - y^2) dx + xy dy,$ bu yerda AB -kesma: $A(2;2), B(3;4).$

59 – variant

1. $\frac{1}{1 \cdot 4} + \frac{1}{2 \cdot 5} + \frac{1}{3 \cdot 6} + \frac{1}{4 \cdot 7} + \dots$
2. $\sum_{n=1}^{\infty} \frac{(3n)!}{(n!)^3 2^{3n}}$;
3. $\sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^{1+\alpha}}, (\alpha > 0)$
4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n \cdot 2^n}$
5. $\sum_{n=1}^{\infty} \frac{(x+1)^n}{(2n-1)!}$
6. $f(x) = e^{-2x}$ funksiyani Makloren qatoriga yoying.
7. $\sqrt{24}, \varepsilon = 0,001$
8. $f(x) = 1 - 2x$ funksiyani $[0, 1]$ da kosinuslar bo'yicha Fur'e qatoriga yoying.
9. $\int_0^1 dy \int_0^{\sqrt{y}} f dx + \int_1^e dy \int_{\ln y}^1 f dx$
10. $\int_1^e \int_1^y \frac{y}{x} dx dy$
- $\iiint_V (9 + 18z) dx dy dz :$
11. $(V): \begin{cases} y = 4x, & y = 0, & x = 1; \\ z = \sqrt{xy}, & z = 0. \end{cases}$
12. $I = \int_{\gamma} \frac{dl}{x^2 + y^2 + 4}$, bu yerda γ - uchlari $O(0;0), A(1;2)$ nuqtalardan iborat kesma.
13. $I = \int_{AB} (4x + y) dx + (x + 4y) dy$, bu yerda $\widehat{AB}$ yoy $y = x^4$ egri chiziqning yoyi: $A(1;1)$ va $B(-1;1)$.

60 – variant

1. $\frac{2}{3} + \frac{2}{3} \cdot \frac{1}{2} + \frac{2}{3} \cdot \frac{1}{3} + \frac{2}{3} \cdot \frac{1}{4} + \frac{2}{3} \cdot \frac{1}{5} + \dots$
2. $\sum_{n=1}^{\infty} \frac{2 + (-1)^n}{n}$;
3. $\sum_{n=2}^{\infty} \frac{1}{n \ln n (\ln \ln n)^2}$
4. $\sum_{n=1}^{\infty} (-1)^{n+1} \cdot \frac{1}{n}$
5. $\sum_{n=1}^{\infty} (n+1)x^n$
6. $f(x) = x \cos 3x$ funksiyani x ning darajalari bo'yicha qatorga yoying.
7. $sh 0,3, \varepsilon = 0,0001$
8. $f(x) = x + 1$ funksiyani $(-1; 1]$ yarim intervalda Fur'e qatoriga yoying.
9. $\int_0^1 dy \int_{-\sqrt{y}}^0 f dx + \int_1^2 dy \int_{-\sqrt{2-y}}^0 f dx$
10. $\int_{-2}^{-1} \int_1^{3+x} \frac{\ln y}{y(x+3)} dx dy$
- $\iiint_V 25y^2 dx dy dz:$
11. $(V): \begin{cases} x = 15, & 3y + z = 1; \\ x = 0, & y = 0, & z = 0. \end{cases}$
12. $I = \int_{\gamma} (x + z) dl$, bu yerda γ egri chiziq parametrik tenglamalari bilan berilgan: $x = 2at\sqrt{1-t^2}, y = a \cdot \ln(1-t^2), z = 2at^2, 0 \leq t \leq \frac{1}{2}$.
13. $I = \int_{\widehat{AB}} y dx - x dy$, bu yerda $\widehat{AB}$ yoy $x^2 + y^2 = 1$ aylananing $A(-\frac{1}{\sqrt{2}}; -\frac{1}{\sqrt{2}})$ nuqtasidan $B(\frac{1}{\sqrt{2}}; \frac{1}{\sqrt{2}})$ nuqtasigacha soat millari harakati yo'nalishida o'tiladi.

ADABIYOTLAR RO'YXATI

1. Claudio Canuto, Anita Tabacco. Mathematical Analysis I, II. Springer-Verlag Italia, Milan 2015, 2010.
2. Soatov Yo.U Oliy matematika. T., O'qituvchi, 1995. 1- 3 qismlar.
3. Д.Писменный. «Конспект лекции по высшей математике», 1,2,3 часть. -М.: Айрис Пресс, 2008.
4. Ю.Ф. Сенчук. Математический анализ для инженеров. 1,2 часть-Харков: НТУ «ХПИ», 2003.- 408 с.
5. Axmedov A.B., Shodmonov G., Esonov E.E., Abdukarimov A.A., SHamsiyev D.N.
Oliy matematikadan individual topshiriqlar. –Toshkent: O'zbekiston ensiklopediyasi, 2014.
6. Xurramov SH. R. Oliy matematika. 1,2-qism. – Toshkent: “Tafakkur” nashriyoti, 2018.
7. Xolmurodov E., Yusupov A.I., Aliqulov T.A. Oliy matematika. 1,2,3-qismlar. –Toshkent: “NEXT MEDIA GROUP”, 2017.
8. John James Stewart. Calculus. Seventh editions. Metric version. Brooks/Cole, Cengage Learning, 2012.
9. Y. Suhov, M. Kelbert. Probability and Statistics by Example. 2nd edition. United Kingdom. University printing house, Cambridge CB2 8BS, 2014.
10. В.Е.Шнейдер, А.И.Слущкий, А.С. Шумов, Краткий курс высшей математики. -М.:, 1978., 1, 2-части.
11. П.Минорский. Сборник задач по высшей математике. ФИЗМАТЛИТ 2010й.
12. А.П.Рябушко и др. Сборник задач индивидуальный заданий по высшей математике. 1, 2-части. – Минск: высшая школа, 1991.

Internet saytlari:

1. [www. ziyonet.uz](http://www.ziyonet.uz);
2. www. gaap.ru;
3. www. cip.com;
4. www. aicpa.ord;
5. www.bilim.uz;

